TOPIC SETS
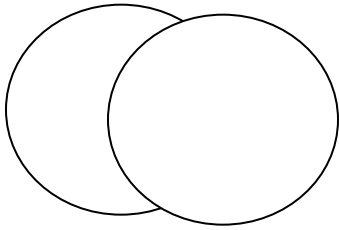**APPLICATION OF SETS**

Examples
1. In a class of 30 pupils 18 like music (M), 21 like Art (A) and some like both.
(a) Represent the above information on a Venn diagram.

(b) How many pupils like both subjects.
Solution
18-x + x +21 – x = 30
18+21-x =30
39-x=30
39-39-x =30-39
-x= -9
$\frac{-x}{-1} = \frac{-9}{-1}$

X = 9

:. 9 Pupils like both subjects

2. In a class of 40 pupils, 20 like mathematics (M), 17 like science (S), 'x' like both
subjects while 8 do not like any of the subjects.
(a) Represent the above information on a Venn diagram.
Solution
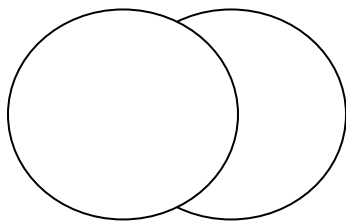
(b) How many pupils like both subjects?
Solution
8+20-x+ x +17- x = 40
28+17-x = 40
45-x = 40
45-45-x = 40-45
-x = -5
$\dfrac{-x}{-1} = \dfrac{-5}{-1}$
X = 5
∴. 5 Pupils like both subjects

(c) What is the probability of selecting a pupil who likes only one subject?
Solution

(20 –x) + (17 – x)
(20-5) + (17-5)   *Prob (only one subject) = $\dfrac{27}{40}$*
15 +12
= 27
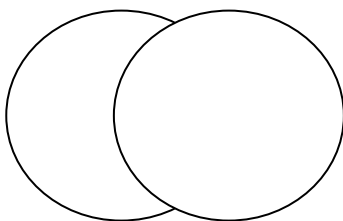
SOLVING PROBLEMS USING VENN DIAGRAMS GIVEN THE UNKNOWN IN THE "DIFFERENCE" REGION

Example 1
In a family of 10 members, 6 members eat meat (M), 5 members eat both meat and fish (F) while 'Y' members eat only fish.
(a) Represent the above information on a Venn diagram
Solution

(b) How many members eat only fish?
Solution

y + 5 + 6 − 5 = 10   y + 6 = 10
y + 6 + 5 − 5 = 10   y + 6 − 6 = 10 − 6
    Y + 6 = 10   **Y = 4**
y + 6 − 6 = 10 − 6
    Y = 4

(c) Find the number of pupils who eat fish.
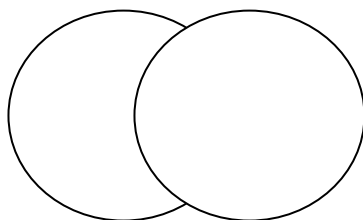> **Solution**
> (y + 5) Pupils
> 4 + 5
> **_9 Pupils_**

> **_Examples 2_**
> In a class of 60 pupils, 25 like swimming (s), x pupils like music (m) only, 20 like both swimming and music and 5 like none of these.
> (a) Represent this information on the Venn diagram.
> > Solution

> (b) Find the value of x.
> > Solution
> > x + 5 + 20 + (25 − 20) = 60
> > x + 25 + 5 = 60
> > x + 30 = 60
> > x + 30 − 30 = 60 − 30
> > **_x = 30_**

> (c) How many pupils like only one type of the activities?
> > Solution
> > x + (25 − 20)
> > 30 + 5
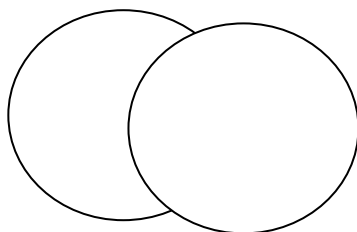> > **_35 pupils_**

SOLVING PROBLEMS USING VENN DIAGRAMS GIVEN ONE OF THE SETS AS UNKNOWN

In a class of 35 pupils, y like mathematics (M), 20 like English (E) while 13 like both subjects.

(a) Using a Venn diagram, show the above information
> **Solution**

(b) Find the number of pupils who like mathematics.

Solution

y − 13 + 13 + 20 − 13 = 35 **OR**   y + 20 − 13 = 35

y + 7 = 35   y + 7 = 35

y + 7 - 7 = 35 − 7   y + 7 − 7 = 35 − 7

_y =28_   **_y = 28_**

OR

y − 13 + 20 = 35

y + 7 = 35

y + 7 − 7 =35 -7

_y = 28_

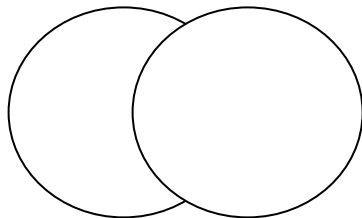**_28 Pupils like mathematics_**

SOLVING PROBLEMS USING VENN DIAGRAMS.
WHEN THE COMPLEMENT OF THE UNION IS NOT GIVEN
Example 1

In a village with 60 farmers, 26 grow rice, 24 grow beans, 10 grow both crops while t grow none of the above.

(a) Represent the above information on a Venn diagram.

Solution

(b) Find the value of t .

Solution

t + 16 + 10 + 14 = 60

t + 40 = 60

t + 40 − 40 = 60 − 40

_t = 20_

SOLVING PROBLEMS USING VENN DIAGRAMS WHEN ONE OF THE SETS IS THE UNIVERSAL

In a group of 40 peoples, they all football, 9 play football only, 15 play tennis, 25 swim and some enjoy all the three games.

   (a) Draw a Venn diagram to represent the above information

Solution

(b) How many people participate in all the three activities?
Solution
15 – p + p + 25 – p + 9 = 40
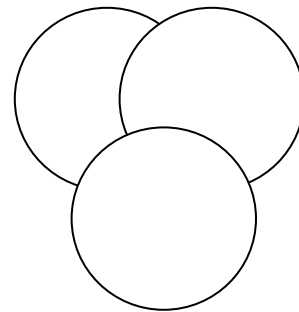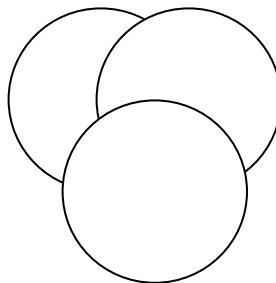15 + 25 – p + 9 = 40
49 – p = 40
49 – 49 – p = 40 -49
-p = -9
<u>-p</u> = <u>-9</u>
-1   -1
_P = 9_
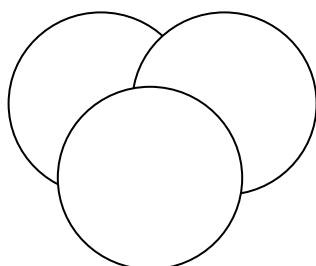<u>9 people participate in the three activities</u>

<u>SETS IN THREE VENN DIAGRAMS DESCRIBING THE SHADED PARTS.</u>
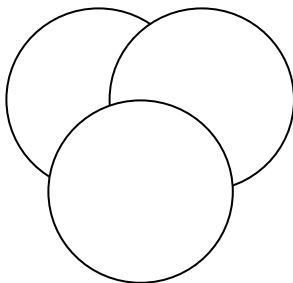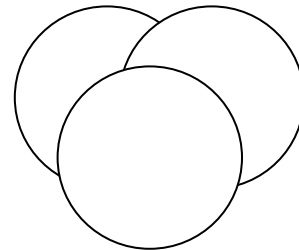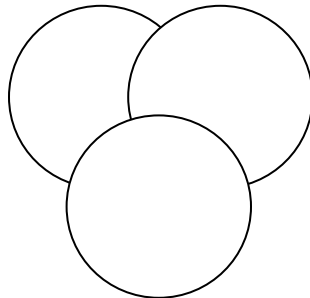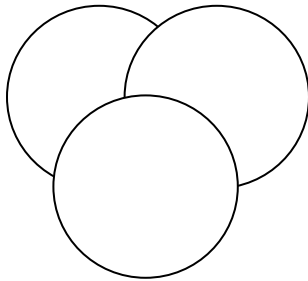
<u>INTERPRETING THREE VENN DIAGRAM SETS</u>
EXAMPLE
The Venn diagram shows the number of pupils who play different games.

Find the number of pupils who play
(a) all the three games.
            __2 pupils__

(b) both volleyball and football.
        __4 + 2 = 6 pupils__

(c) volleyball and hockey only.
        __5 pupils__

(d) only one game.
        __3 + 8 + 6 = 17 pupils__

(e) Hockey.
        __5 + 2 + 1 + 8 = 16 pupils__

(f) Football only.
        __6 pupils__

(g) Football and hockey but not volleyball.
        __1 pupil__

COMPLETING 3 VENN DIAGRAM SETS WITH MISSING INFORMATION
EXAMPLE
In the Venn diagram below, 20 pupils like mathematic (M), 16 pupils like English (E), 30 pupils like science (S) .complete the Venn diagram with missing information.
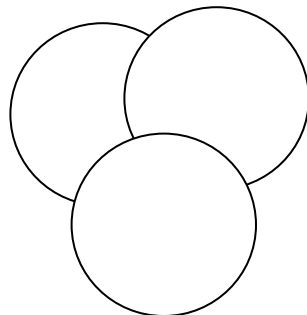
n(M) only	n(E) only	n(S) only	n(MUSUE) ´
20 – (3 + 2 + 6)	16 – (3 + 2 + 5)	30 – (6 + 2 + 5)	55 – (20 + 6 + 17 + 5)
20 -11	16 – 10	30 – 13	55- 48
__9__	__6__	__17__	__7__

REPRESENTING INFORMATION ON A VENN DIAGRAM OF THREE SETS
EXAMPLE

At a birthday party, 11 people took Fanta (F), 13people took Mirinda (M) and 15 people took pepsicola. Given also that 2 people took all the three types of drinks, 1 per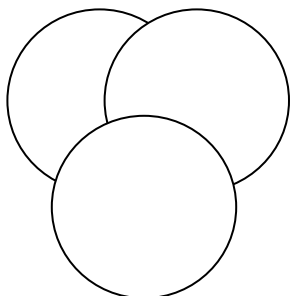son took both Fanta and Mirinda only, 3 people took both Fanta and Pepsi only ,6 people took both Pepsi and Mirinda only.

Represent the above information on Venn diagram and complete the Venn diagram with missing information.

n(F) only	**n(P) only**	**n(M) only**
11 - (3 + 2 + 1)	15 – (3 + 2 + 6)	13 – (6+ 2+ 1)
11 – 6	15 -11	13 -9
5	**4**	**4**

Example 2

In a class of 35 pupils, 20 like mathematics (M), 19 like science (S) and 19 like English (E) if; 10pupils like both mathematics and science,
11 like both science and English
9 like both English and mathematics
7 like all the three subjects.
Represent the above information on a Venn
Diagram
Solution
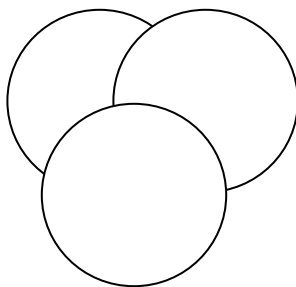
n (∑) = 35   n (MnS) only = 10 – 7
n (M) = 20   = 3
n (S) = 19   n(SnE) only = 11 – 7

n (E) = 19   = 4
n (MnSnE) = 7   n(EnM) only = 9 – 7
n (MnS) = 10   = 2
n (SnE) = 11   n(M) only = 20 – 12
n (EnM) = 9   = 8
                         n(S) only = 19 – 14
                                             = 5
                         n(E) only 19 – 13
                                             = 6

n(MnS) only	n(SnE) only	n(EnM) only	n(M) only	n(S) only	n(E) only
10 -7	11 – 7	9 – 7	20 – 12	19 -14	19 -13
3	**4**	**2**	**8**	**5**	**6**

SHARING IN RATIOS GIVEN TOTAL SHARE
Example 1
Share 18 mangoes in the ratio of 4:5.

Solution	1st share	2nd share
Total ratio	$(4 \times \frac{18^2}{9})$ mangoes	$(5 \times \frac{18^2}{9})$ mangoes
4 + 5		
9	(4 x 2) mangoes	(5 x 2) mangoes
	8 mangoes	**10 mangoes**

Example 2
Sh. 60,000 was shared among three sisters, Anne, Betty and Claire in the ratio 1:2:3 respectively.
How much did each get?

Solution	Anne's share	Betty share	Claries share
Total ratio.	10000	10000	10000
1 + 2 + 3	$1 \times \frac{60000}{6}/=$	$2 \times \frac{60000}{6}/=$	$3 \times \frac{60000}{6}/=$
6			
	1 x 10000/=	2 x 10000/=	3 x 10000/=
	_10000/=_	**_20000/=_**	**_30000/=_**

SHARING IN RATIOS GIVEN THE SHARE OF ONE PERSON.
Example 1
Paul and James shared some money in the ratio of 3:5 respectively. If James got 3000/= ,

(a) Find Paul's share
Solution

Paul : James   5 parts represent 3000/=

3   : 5   1 part represent $\dfrac{3000/= \times 3}{5}$

?   : **3000/=**

                   3 part represent $\dfrac{3000/= \times 3}{5}$

                         = 600/= x 3

                     = 1800/=

(b) What was their total share?
Solution

Pupils share = 1800/=   OR   Let x represent total share

James' share = 3000/= $\dfrac{5}{8}$ x X = 3000/= x 8

Total share = 4800/=

                      8 x $\dfrac{5x}{8}$ = 3000/= x 8

                      5x = $\dfrac{3000/= \times 8}{5}$

                      X = 600 x 8

                      X = 4800/=

SHARING IN RATIOS GIVEN DIFFERENCE RATIOS

Example1

A and B shared money in the ratio of 3:7 respectively. If B got shs 4000 more than A,

(a) Find the share of A
Solution

A: B   Difference in ratio

3:7   7 – 3

          4

4 parts represent 4000/=

1 part represents $\dfrac{4000/=}{4}$ = 1000/=

3 parts represent 3 x 1000/=

              3000/=

(b) Find their total share.
Solution

Total = 3 + 7

$$= 10$$

4 parts represent 4000/=

1 parts represent $\underline{4000/=}$
                        4

10 parts represent 10 x 1000/=
       = 10000/=

Example 2

Lucy and Danny shared some money in the ratio of 2:5 respectively. If Lucy got 1500/= less than Danny, how much did Danny get?

Solution

Lucy : Danny
2   : 5
Difference in ratio = 5 – 2
  = 3

3parts represent 1500/=
1part represents $\underline{1500/=}$
                        3
5parts represent 5 x 500/=
= 2500/=

SHARING IN RATIOS, APPLICATION IN PERIMETER OF RECTANGLES
Examples

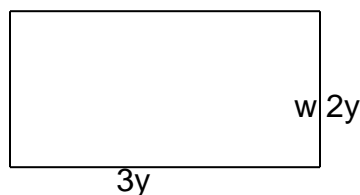The ratio of the length to the width of a rectangle is 3:2 respectively. If the perimeter of the rectangle is 40cm.

(a) Find the actual length and width of the rectangle
Solution
Let y represent 1 part
Length =   3y
Width =   2y

w 2y

3y

$2l + 2w = p$
$(2 \times 3y) + (2 \times 2y) = 40cm$
$6y + 4y = 40cm$
$10y = 40cm$
$\dfrac{10y}{10} = \dfrac{40cm}{10}$
Y = 4cm

Length = 3 x y
    = 3 x 4cm
    = **12cm**

width = 2 x y
    = 2 x 4cm
    = **8cm**

(b) Find the area of the rectangle
Solution
Area = L x W
    = 12cm X 8cm
    = 96cm²

ADDITION AND SUBTRACTION OF DECIMALS

a. Simplify 2.62 + 14 + 6.4

Solution

```
  2.62
+ 14.00
   6.40
 23.02
```

b. Subtract 0.99 from 2

solution

```
 2.00
 0.99
 1.01
```

MULTIPLICATION OF DECIMALS

a. Multiply: 1.3 x 1.2

Solution

$= \dfrac{13}{10} \times \dfrac{12}{10} = \dfrac{156}{100}$

$= \textbf{\textit{1.56}}$

b. Work out: 2.45 x 0.25

solution

$= \dfrac{245}{100} \times \dfrac{25}{100} = \dfrac{6125}{10000}$

$= \textbf{\textit{0.6125}}$

DIVISION OF DECIMALS

Divide 0.72 ÷ 0.9

Solution

$0.72 \div 0.9 = \dfrac{72}{100} \div \dfrac{9}{10}$

$= \dfrac{72}{100} \times \dfrac{10}{9}$

$= \dfrac{8}{10}$

$= \textbf{\textit{0.8}}$

How many 1.5 metre pieces can be cut from a length of 7.5 metres?

Solution

$(7.5) \text{ m} \div 1.5\text{m} = \dfrac{75}{10} \div \dfrac{15}{10}$

$= \dfrac{75}{10} \times \dfrac{10}{15}$

$= \textbf{5 pieces}$

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COMBINED OPERATIONS ON DECIMALS

Simplify; $\dfrac{3.2 - 0.08}{0.2 \times 0.3}$

Solution

3.20	= $\frac{2}{10}$ x $\frac{3}{10}$	= $\frac{312}{100}$ ÷ $\frac{6}{100}$
0.08		
_3.12_	= $\frac{6}{100}$	= $\frac{312}{100}$ x $\frac{100}{6}$
	= **_0.06_**	= **_52_**

Work out: - $\frac{0.28 \text{ x } 0.81}{027 \text{ x } 4.2}$

Solution

$\frac{28}{100}$ x $\frac{81}{100}$ $\frac{27}{100}$ x $\frac{42}{10}$

$\frac{28}{100}$ x $\frac{81}{100}$ x $\frac{100}{27}$ x $\frac{10}{42}$

$\frac{2}{10}$ $\frac{2 \text{ x } 1 \text{ x } 1 \text{ x } 1}{10 \quad \text{ x } 1 \text{ x } 1}$

         _0.2_

EXPRESSING FRACTIONS AS RECURRING DECIMALS

Express $\frac{2}{3}$ as a decimal

Solution

Expressing recurring decimals as fractions

Change 0.33----to a fraction

Solution

M = 0.33 ----------- (i)

10m = 0.333 --- x 10

10m = 3.333 ----- (ii)

-10m = 3.333 ---

  M =0.333 ----

  9m = 3

$\frac{9m}{9}$ = $\frac{3}{9}$

M =⅓

Express 0.122 – to a common fraction
Solution
Let x represent the fraction
    X = 0.1222 ------ (1)
10 x X = 0.1222 ------ x 10
    10x = 1.222 -------- (ii)
10 x 10x = 1.222 -----x 10
100x = 12.222 ------- (iii)
100x = 12.222 ------- (iii)
10x = 1.222 --------- (ii)
    90x = 11

    90x = 11
    90   90
X = 11
    90

ADDITION AND SUBTRACTION OF FRACTIONS

Work out: - $\frac{5}{6} - \frac{1}{3} + \frac{1}{2}$

 Solution

$= \frac{5}{6} - \frac{1}{3} + \frac{1}{2} = \frac{5 + 3 - 2}{6}$

$= \frac{8 - 2}{6}$

$= \frac{4}{6}$

$= \frac{2}{3}$

solution

$= \frac{2}{1} - \frac{1}{3} + \frac{1}{4}$ $= \frac{24 + 3 - 5}{12}$

$= \frac{27 - 4}{12}$

$= \frac{23}{12}$

1 11
12

MULTIPLICATION AND DIVISION OF FRACTIONS

1.   Multiply: - $2\frac{1}{4} \times 1\frac{1}{5}$

15

Solution

$2\frac{1}{4} \times 1\frac{1}{5} = \frac{9}{4} \times \frac{6}{5}$

$= \frac{9 \times 3}{2 \times 5}$

$= \frac{27}{10}$

$= 27$

2. Work out: - $1\frac{1}{4} \div 1\frac{3}{5}$

solution

$1\frac{1}{4} \div 1\frac{3}{5} = \frac{5}{4} \div \frac{8}{5}$

$= \frac{5}{4} \times \frac{5}{8}$

$= \frac{25}{32}$

3. How many $1\frac{2}{3}$ are contained in

solution

$15 \div 1\frac{2}{3}$

$= 15 \div \frac{5}{3}$

$= 15 \times \frac{3}{5}$

$= 3 \times 3$

COMBINED OPERATIONS
BODMAS

1. Simplify $\frac{1}{3}$ of $(\frac{1}{2} - \frac{1}{4}) + \frac{7}{12}$

Solution
BODMAS

$\frac{1}{3}$ of $(\frac{2-1}{4}) + \frac{7}{12}$

$\frac{1}{3}$ of $\frac{1}{4} + \frac{7}{12}$

$\frac{1}{3} \times \frac{1}{4} + \frac{7}{12}$

$\frac{1}{12} + \frac{7}{12}$

$\frac{8}{12}$

$\frac{2}{3}$

APPLICATION OF FRACTIONS
2/3 of a class are girls, if there are 20 girls in that class;
(a) Find the total number of pupils in the class.
Solution
Let x represent the total

$\frac{2}{3}$ of x = 20

$\frac{2}{3} \times X = 20$

$3 \times \frac{2X}{3} = 20 \times 3$

$\frac{2X}{2} = \frac{20 \times 3}{2}$

X = 30

(b) Find the number of boys
Solution

Fraction of boys = $1 - \frac{2}{3}$ Number of boys = $\frac{1}{3} \times 30$

$= \frac{3}{3} - \frac{2}{3}$

$= \frac{1}{3}$ = 1 x 10

                                                  = 10boys

No of boys = 30 – 20
         =   10boys

APPLICATION OF FRATIONS

(1)   After covering 2/3 of a journey, a motorist still had 40km to cover. How long was the whole journey?

Solution

Fraction covered	Fraction left	Let whole journey
$\dfrac{2}{3}$	$1 - \dfrac{2}{3}$	$\dfrac{1}{3}$ of y = 40km
	$\dfrac{3}{3} - \dfrac{2}{3}$	$\dfrac{1}{3}$ x y = 40km
	$\dfrac{1}{3}$	3 x $\dfrac{y}{3}$ = 40km x 3
		Y = 120k

2. Ina group, 1/6 are girls and there are 8more boys than girls.

(a)Find the total number of pupils in the group.

Solution

Fraction of boys = $1 - \dfrac{1}{6}$

$= \dfrac{6}{6} - \dfrac{1}{6}$

$= \dfrac{5}{6}$

Fraction of more boys = $\dfrac{5}{6} - \dfrac{1}{6}$

$= \dfrac{4}{6}$

Let the total number be x

$\dfrac{4x}{6} = 8$

$6 \times \dfrac{4x}{6} = 8 \times 6$

$\dfrac{4x}{4} = \dfrac{8 \times 6}{4}$

x = 2 x 6

x = 12

There are 12 pupils in the group.

(b)How many girls are in the group?

Solution

$\dfrac{1}{6}$ x 12

2girls

APPLICATION OF FRACTIONS.
Finding remainders: -   Given one fraction
                         Given two fractions

1. $\frac{4}{5}$ of the class are boys and the rest are girls.

Find the fraction of girls.

Solution

$1 - \frac{4}{5}$

$\frac{5}{5} - \frac{4}{5}$

$\mathbf{\frac{1}{5}}$

2. $\frac{1}{4}$ of the animals are cows, $\frac{1}{3}$ are bulls and the rest are goats.

Solution

$1 - (\frac{1}{4} + \frac{1}{3})$

$1 - \frac{3 + 4}{12}$

$1 - \frac{7}{12}$

$\frac{12}{12} - \frac{7}{12}$

$\mathbf{\frac{5}{12}}$

APPLICATION OF FRACTIONS (finding fraction of the remainder)

1. On a farm, $\frac{2}{3}$ of the animals are black, ¼ of the remainder are brown.

(a) Find $\frac{1}{3}$ of the fraction left

Solution

Black	Remainder	Brown	Fraction Left	1 Fraction Left
$\frac{2}{3}$	$1 - \frac{2}{3}$	$\frac{1}{3} \times \frac{1}{4}$	$\frac{1}{3} - \frac{1}{12}$	$\frac{1}{3} \times \frac{1}{4}$
	$\frac{3}{3} - \frac{2}{3}$	$\frac{1}{12}$	$\frac{4-1}{12}$	$\frac{1}{12}$
	$\frac{1}{3}$		$\frac{3}{12}$	
			$\mathbf{\frac{1}{4}}$	

(b) Find 1/5 of the fraction left

$\frac{1}{5}$ of $\frac{1}{4}$

$\frac{1}{5}$ x $\frac{1}{4}$

$\frac{1}{20}$

MORE ABOUT APPLICATION OF FRACTIONS

John spent 1/3 of his money on books and 1/6 of the remaindes on transport.

(a)   What fraction of his money was left?

Solution

Books	**remainder**	**transport**	**fraction left**
$\frac{1}{3}$	$1 - \frac{1}{3}$	$\frac{1}{6}$ of $\frac{2}{3}$	$\frac{2}{3} - \frac{1}{9}$ or $1 - (\frac{1}{3} + \frac{1}{9})$
	$\frac{2}{3}$	$\frac{1}{6}$ x $\frac{1}{3}$	$\frac{6-1}{9}$ $1 - \frac{3+1}{9}$
		$\frac{1}{9}$	$\frac{5}{9}$ $1 - \frac{4}{9}$
			$\frac{9}{9} - \frac{4}{9}$
			$\frac{5}{9}$

(b)   If he left with sh. 15000 how much did he have at first.

Solution

Let the total be x

$\frac{5}{9}$ x X = 15000/=

9 x $\frac{5x}{9}$ = 15000/= x9

$\frac{5x}{5}$ = $\frac{15000/= \times 9}{5}$

x = 3000/= x 9

x = 27000/=

TAPS

1.   Tap A can fill a tank in 6 minutes and tap B can fill the same tank in 3 minutes. How long will both taps take to fill the tank if they are opened at the same time?

Solution

In one minute

Tap A fills 1/6 of the tank

Tap B fills 1/3 of the tank

Both taps fill (1/6 + 1/3) of the tank

$= \frac{1 + 2}{6}$	total time taken of fill tank
	$= (1 \div \frac{1}{2})$ minutes
$= \frac{3}{6}$	$= (1 \times \frac{2}{1})$ minutes
$= \underline{1}$	**= 2minutes**

2.   Tap A takes 3 minutes to fill a tank and tap takes 4 minutes to draw water from the tank.

How many minutes will it take to fill the tank if both taps are left running?

Solution

In 1 minute   total time taken to fill the tank

Tap A fills $\frac{1}{3}$ of the tank $1 \div \frac{1}{12}$

Tap B empties $\frac{1}{4}$ of the tank $1 \times \frac{12}{1}$

Bothe taps fill $(\frac{1}{3} - \frac{3}{4})$ of the tank   **12 minutes**

$\frac{4-3}{12}$

$\mathbf{\frac{1}{12}}$

3.   Tap A and B are connected to a tank. Tap A can fill the tank in 3 minutes. Ta\p B draws water from the tank. When both taps are running, if takes 12 minutes for the tank to be filled . How long does tap B take to draw water from the tank?

Solution

In 1 minute, tap A fills $\frac{1}{3}$ of the tank

In I minute both taps fill $\frac{1}{12}$ of the tank

In 1 minute tap B empties $\frac{1}{3} - \frac{1}{12}$ of the tank

$\frac{4-1}{12}$

$\frac{3}{12}$

$\mathbf{\frac{1}{4}}$

Total time taken to draw water from the taken

$(1 \div \frac{1}{4})$

$1 \times \frac{4}{1}$

4 minutes

PERCENTAGES
APPLICATION OF PERCENTAGES

1 Opio has 400 heads of cattle. 80% of them are cows and the rest are bulls.

Find the number of cows.
   Solution
   $\frac{80}{100}$ X 400 = 80 X 4

                = 80 x 4
                = 320 cows

(a) Find the percentage of bulls.
   Solution
   100% - 80%
   20%

(b) What is the total number of bulls?
   Solution
   $\frac{20}{100}$ x 400 = 20 x 4

                = **80 bulls**

   OR
    400
   - 320
     80bulls

2. If 30% of my salary is spent on food, 1 save sh. 21000. What is my salary?
   %age saved = 100% - 30%
                70% $\frac{70}{100}$ x y = 21000/=
   70% represent 21000/=
   1% represents $\frac{21000/=}{70}$ 10 x $\frac{7y}{10}$ = 21000/= x 10

   100% represents $\frac{21000 \times 100}{70}$ $\frac{7y}{7} = \frac{210000}{7}$

                = 300 x 100   **y = 30000/=**
                = 30000/=

PERCENTAGE INCREASE AND DECREASE

1. Increase sh,800 by 20%

Solution

New % = 100% + 20%   increase
            120%   20% of 800/=

New amount 120 x 800/=   20 x 800/=
              100   100

              120 x 8   20 x 8
              = 960/=   **= 160/=**

                        New amount
                            800/=
                        + 160/=
                            960/=

2. Increase sh.2000 by 10% then by 20%

    Solution

    Method 1

10% increament	new amount	20% increament	new amount
10 x 2000	2000	20 x 2200	2200
100	+ 200	100	+ 440
10 x 20/=	**2200/=**	20 x 22	**2640/=**
200/=		**440/=**	

Method 2

1st increament   = 100% + 10%
                  = 110%
2nd increament   = 100% + 20%
                  = 120%
New amount   = 110 x 120 x 2000
                      100   100
                  = 11 x 120 x 2/=
                  = 1320 x 2/=
                  = **2640/=**

3. Decrease sh.12000 by 10%

Solution

New % = 100% - 10%
      =   **90%**

90 x 1500/=
100
90 x 15
1350/=

4. Decrease sh. 12000 by 5% then by 10%

   Solution

   100% - 5% (5% reduction)

   100% - 10% (10% reduction)

   $\dfrac{95}{100}$ x $\dfrac{90}{100}$ x 12000

   95 x 9 x 12/=

   10260/=

FINDING ORIGINAL NUMBER AFTER INCREASE

1. What amount when increased by 20% becomes sh.1440?

   Solution

   After increase the new percentages

   Method 1

   100% + 20% = 120%

   120% rep 1440

   1% rep $\dfrac{1440}{120}$

   100% rep 100x $\dfrac{1440}{100}$

   100 x 12

   1200/=

   Method 2

   Let the amount be x

   (100% + 20%) of x = 1440/=

   100 x $\dfrac{120}{100}$ x X = 1440 x 100

   $\dfrac{120x}{120} = \dfrac{144000}{120}$

   x = 1200/=

2. When the prices of a radio was increased by 30% it becomes sh.16900. What was the old price?

   Method 1

   New % = 100% + 30%

       = 130%

   130% rep sh 16900

   1% rep sh $\dfrac{16900}{130}$

       = 130

   100% rep 100 x 130/=

       = 13000/=

   method 2

   let the salary be y

   100% + 30% = 130%

   $\dfrac{130}{100}$ x y = 16900

   100 x $\dfrac{130y}{100}$ = 16900 x 100

   $\dfrac{130y}{130} = \dfrac{16900 \times 100}{130}$

   Y = 13000/=

FINDING ORIGINAL NUMBER AFTER DECREASE

1. If a man's salary is decreased by 35% it becomes sh.15600. what is his salary?

   Solution

   Method 1

   100% - 35% = 65%

   65% rep 15600/=

   1% rep $\dfrac{15600/=}{65}$

   100% rep 100 x $\dfrac{15600}{65}$

   100 x 240

     24000/=

   method 11

   100% - 35% = 65%

   let the salary be x

   $\dfrac{65}{100}$ of x = 15600/=

   100 x $\dfrac{65x}{100}$ = 15600 x 100

   65x = $\dfrac{15600 \times 100}{65}$

X = 24000/=

2.   When the price of a radio is reduced by 25% it becomes sh.67500. what was the old price of the radio?

Solution

Method 1   method 2

New % = 100% - 25%   new % = 100% - 25%

          75%   75%

75% rep 67500/=   Let the old price be x

1% rep 67500/=   75 x X = 67500/=

          75   100

     900/=   100 x 75x = 67500 x 100

                                                      100

100% rep 100 x 900/=   75x = 6750000

     90,000/=   75   75

                                               X = 90,000/=

FINDING PERCENTAGE OF INCREASE OR DECREASE

1.   Where 400kg are increased by p% they become 440kg. Find the value of p.

Solution

Increase = 440kg

          -400kg

            40kg

(40kg x 100)%

  400kg

10%

P = 10%

2.   800 pupils where decreased by y% to 680 pupils. find the value of y.

Solution

Decrease = 800   y = (Decrease x 100)

          -680   Old no

          120   y = 120 x 100

                                           y = 15%

PERCENTAGE PROFIT AND LOSS

The idea of increase can also give the same meaning as: gain, profit or raise.

1.   An article was bought at sh. 100,000 and sold at sh.120000. calculate the percentage profit

Solution

Profit = sp – cp   % profit = (Profit x 100) %

     = 120,000 – 100,000/=   B.P

     = 20,000/=   = (20000 x 100) %

                                                   100000

= 20%

2.   Otim bought a shirt at sh. 4000 and sold it at sh.3000. Find his percentage loss.

Solution

Loss = 4000/= - 3000/=   % loss = $\frac{\text{loss} \times 100}{\text{B.P}}$ %

          = 1000/=

                            = $\frac{1000 \times 100}{4000}$ %

                            = 25%

FINDING SELLING PRICE GIVEN PERCENTAGE PROFIT OR LOSS AND BUYING PRICE

1.   Birigwa bought a DVD player at sh. 300,000 and sold it at 10% profit. Find his selling price.

      Solution new % = 100% + 10%

                        = **110%**

      $\frac{110}{100}$ x 300000/=

      330000/=

2.   A fridge bought for sh.600,000 was sold at a loss of 25%. Calculate the selling price.

      Solution new % = 100% -25%

                        = 75%

      New amount   = $\frac{75}{100}$ x 60000/=

                    = 75 x 6000/=

                    = 450000/=

FINDING COST PRICE GIVEN PERCENTAGE PROFIT OR LOSS AND SELLING PRICE

1.   By selling a blanket at sh. 36000, a trader made a profit of 20%. Calculate the cost price of the blanket

Solution

New % = 100% + 20%

        = 120%

Cost price % = 100%

120% rep 36000/=

1% rep $\frac{36000/=}{120}$

100% rep 100 x $\frac{36000/=}{120}$

        = 30000/=

2. A dealer sold a bicycle for sh. 45000 there by losing 10%
(a) Calculate the original price of the bicycle.
Solution
New % = 1000% - 10%
      = 90%

Original % = 100%
90% rep = 45000/=
1% rep = 45000/=
         90
100% rep 100 x 500
      = 50000/=

(b) How much did he lose
Solution
10 x 50000/=
100
= 5000/=

DISCOUNT

Discount is realized when a trader sells an item at a price less than the marked price.

1. The marked price of a book is sh.4000. If a customer is offered a 10% discount:
(a) How much is the discount?
Solution
= 10 x 4000/=
  100
= 10 x 40
= **400/=**

(b) How much does the customer pay?
Solution

4000/=	or new % = 100% - 10%	90 x 40
- 400/=	= 90%	**3600/=**
3600/=	= 90 x 4000/=	
	= **3600/=**	

2. The marked price of a shirt was sh. 1500. After a discount a customer paid sh.1200.how much was the discount
Solution
Discount = marked price – cash price
         = 1500/= - 1200/=

= 300/=

(a)   Calculate the percentage discount.

Solution

% discount = (Discount x 100) %

               Marked price

         = (300 x 100) %

             1500/=

      = 20%

FINDING THE MARKED PRICE (ORIGINAL PRICE)

1.   Cissy paid sh. 18000 for a hand bag after being offered a discount of 10%.
    Calculate the marked price of the bag?

New % = 100% - 10%

     =   90%

90% rep 18000/=

1% rep 18000

       90

100% rep = 100 x 200

       = 20000/=

(c)   How much was the discount

20000/=   or Discount = 10 x 20000/=

-18000/=   100

  2000/=   = 10 x 200

                     = 2000/=

COMMISSION

1.   A salesman was paid a salary of sh.10000 plus a commission of 10% of the
    value of goods sold. If he sold goods worth sh 6500, how much did he earn
    altogether?

Solution

Salary = 10000/=

Commission = 10 x 6500

           100

        = 650/=

Total amount earned = 10000

                  + 650

               10650/=

2. Kamara was given a commission of 3% of his sales. How much did he earn if he sold 50 toys at sh. 15000 each?

Solution

Total sales = 80 x 15000/=

= 1,200,000/=

His commission = $\frac{3}{100}$ x 1200, 000/=

= **36,000/=**

SIMPLE INTREST

1. Calculate the simple interest on sh.8000 for 2yrs at 10% per annum

Solution

S.I = PTR

= 8000 x 2 x $\frac{10}{100}$

= 80 x 20

= **1600/=**

2. Calculate the simple interest on sh.24000 for 8 months at simple interest rate of 15% per year.

Solution

S.I = PTR

= 24000 x $\frac{8}{12}$ x $\frac{15}{100}$

= 20 x 8 x 15

= **2400/=**

3. Calculate the simple interest on sh. 24000 for 8 months at a simple interest rate of 2% per month.

Solution

S.I = PTR

= 24000 x 8 x $\frac{2}{100}$

= 240 x 16

= **3840/=**

FINDING RATE, PRINCIPAL OR TIME

1. Nabifo deposited sh.50000 on her saving s account. At the end of 3yrs the simple interest earned was sh.15000. Calculate the rate of interest.

Solution

PTR = I

50000 x 3 x $\frac{R}{100}$ = 15000

$\frac{1500R}{1500}$ = $\frac{15000}{1500}$

R = 10%

2.   Calculate the rate of interest if sh.30000 can yield a simple interest of sh.1125 in 9months.
Solution
P x T x R = I
30000 x 9 x R = 1125
     12 100
75 x 3 x R = 1125
75 x 3   75 x 3

R = 5%

3.   In what time will sh.1200 yield an interest of sh. 1800 at per year?
Solution
P x T x R = I
12000 x T x 5__ = 1800
      100
600T = 1800
600   600
T= 3years.

COORDINATES
INTRODUCTION
Identifying lines of a coordinate graph
Identify all possible lines on the grid below;
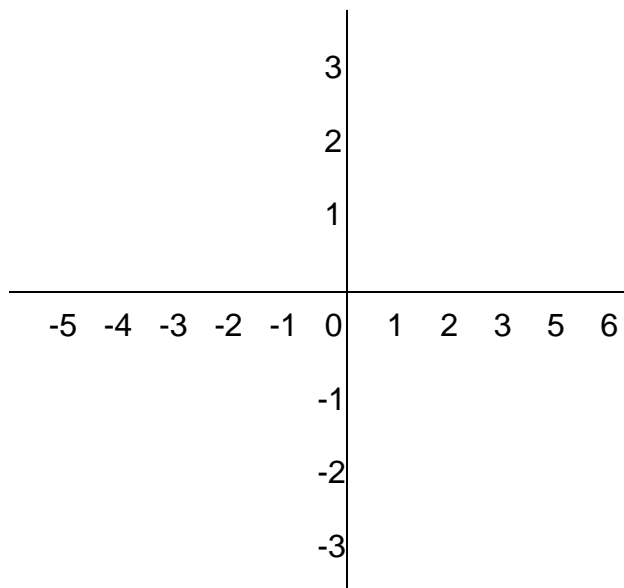
PLOTING GIVEN POINTS
Plot the following point on a grid
A(0,5), B(0,-4) C(3,0), D(-4,0) E(-2,-2) F(-3,-5) G(+2,-4), H(-5,+1) etc.

```
                          5
                          4
                          3
                          2
                          1
 -6 -5  -4  -3  -2  -1   0|  1  2  3  5  6
                         -1
                         -2
                         -3
                         -4
```
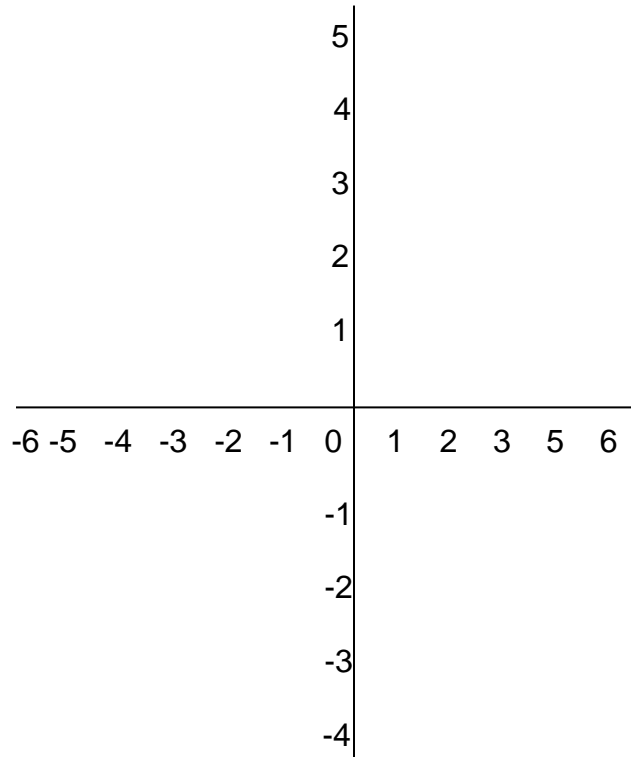
NAMING PLOTTED POINTS
Name the various points on the coordinate graph.

```
                          5
                          4
                          3
                          2
                          1
 -6 -5  -4  -3  -2  -1   0|  1  2  3  5  6
                         -1
                         -2
                         -3
```
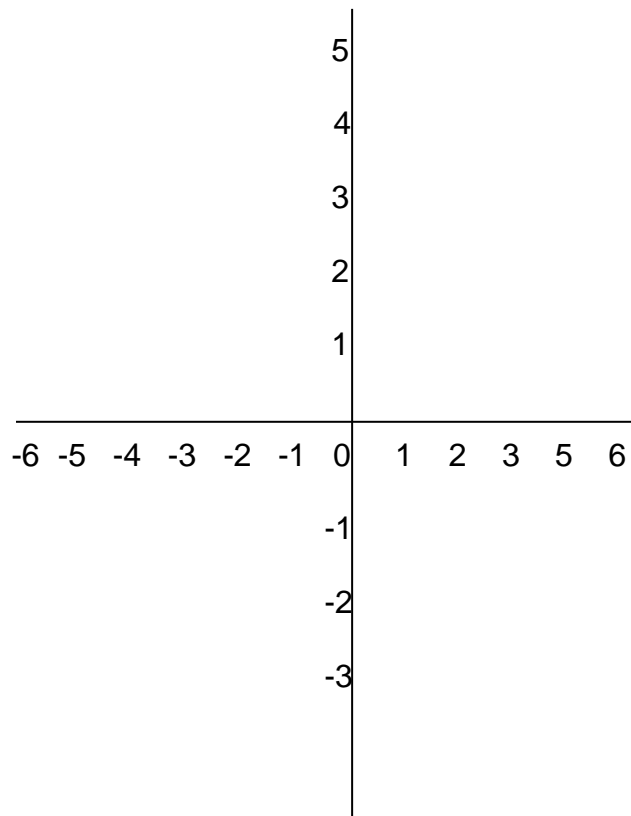
FORMING FIGURES

On the grid below plot the following points

U(-1,4), V(3,4), W(7,-2) and X(-1,-2)

```
                    5
                    4
                    3
                    2
                    1

 -3  -2  -1   0|   1   2   3   5   6   7   8   9
                   -1
                   -2
                   -3
```
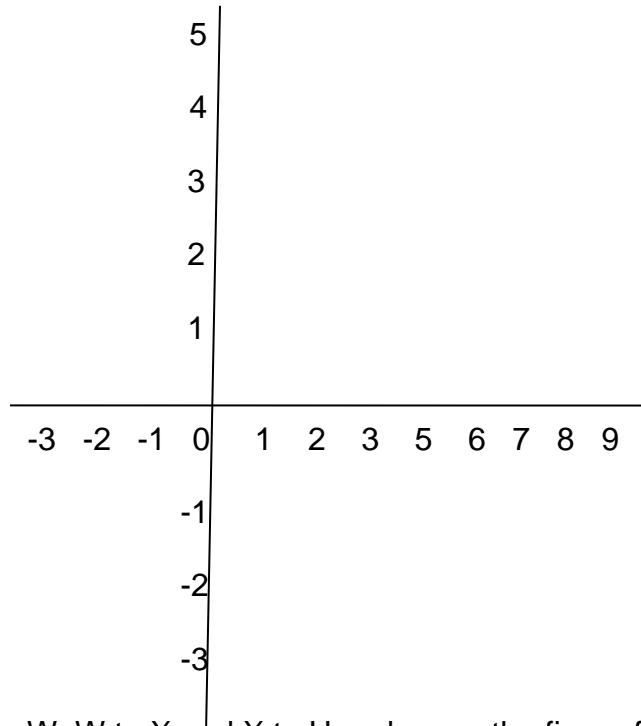
Join point U, to V, V to W, W to X and X to U and name the figure formed .

A trapezium

(i)   Find its area.

Area = $\frac{1}{2}$h (a + b)

$\frac{1}{2}$ x 6units (4units + 8units)

3units x 12units

= **36square units**

(ii)   If each small square represents a cm, work out the area of the above figure

Area = $\frac{1}{2}$h (a + b)

1 x6cm (4cm + 8cm)

3cm x 12cm

= **36cm²**

USING EQUATION OF THE LINE TO COMPLETE TABLES

1.   Given that y = x + 1, complete the table below.

X	-3	__	-1	__
Y	- 2	-1	__	1

2.   Given that y = x - 2, complete the table below.

Y	- 4	---	- 2	---
X	- 2	- 1	---	1

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TRAVEL GRAPHS
READING HORIZONTAL AND VERTICAL SCALES.
- Identification of horizontal and vertical axis
- Interpreting and reading scales correctly study the travel graph below and answer the questions that follow.
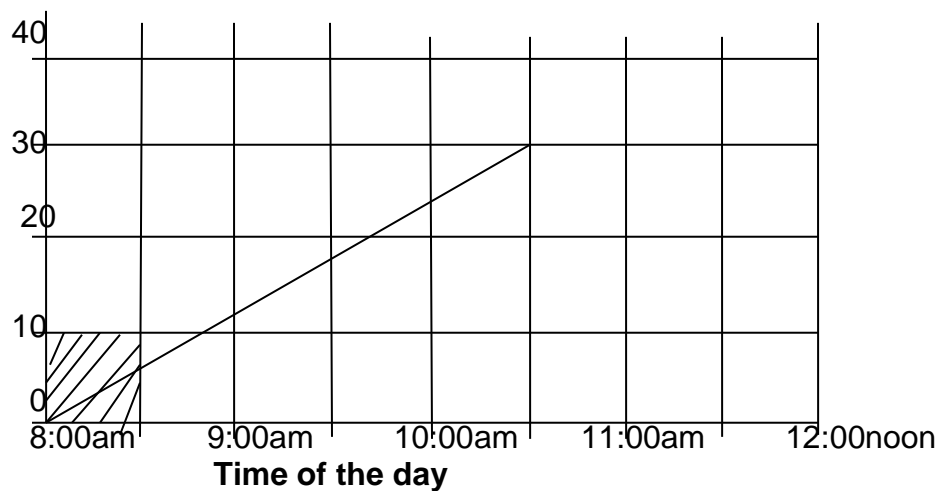
Time of the day

1. What is shown on the
(i) Vertical axis?
    <u>Distance in km</u>

(ii) Horizontal axis?
     <u>Time of the day</u>

2. What is the scale on the
(i) vertical axis?
    <u>I small sq rep. 5km</u>

(ii) horizontal axis?
     <u>I small sq rep 30minutes</u>

INTERPRETING DRAWN TRAVEL GRAPHS

The travel graph below shows a journey of a motorist, use it to answer questions that follow.
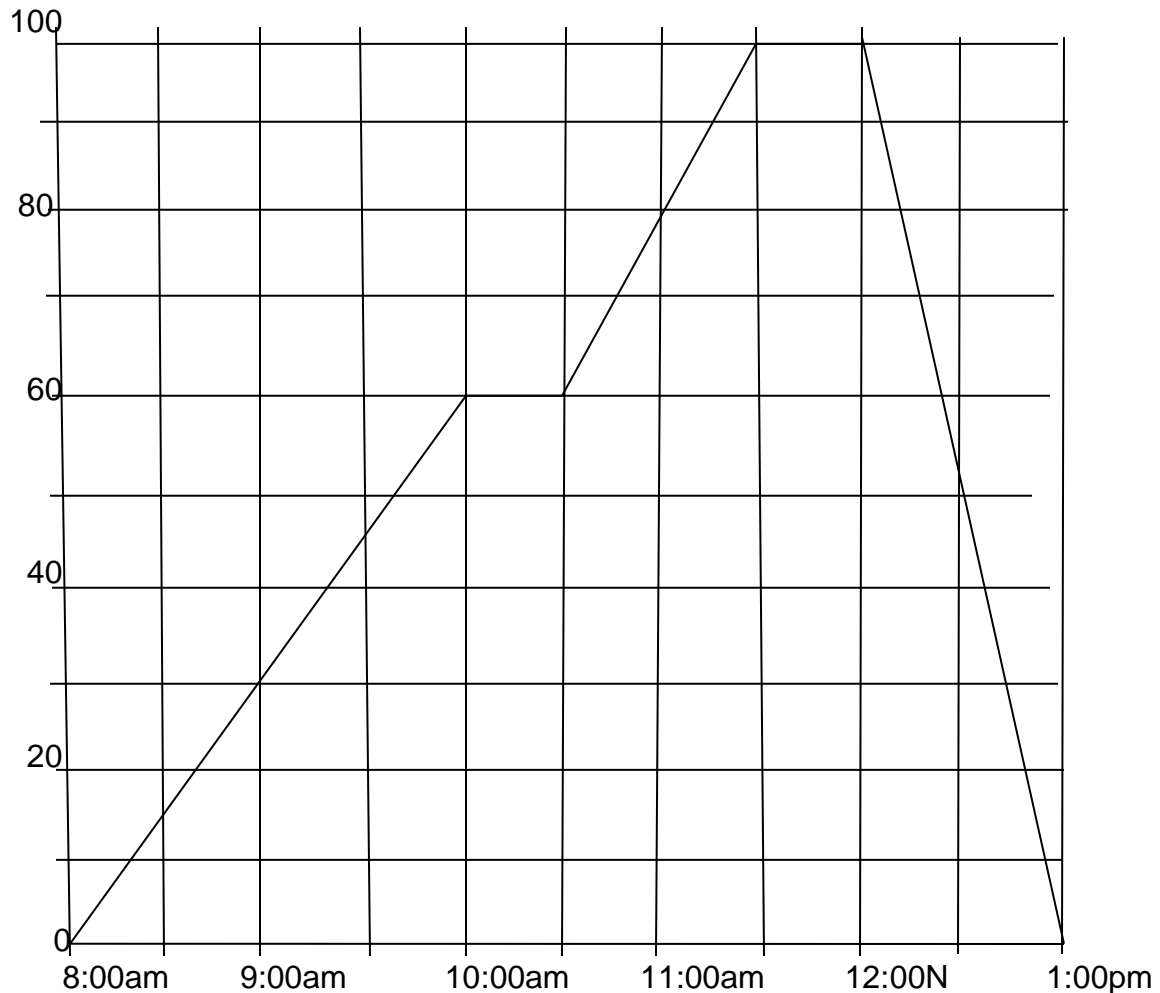
a. At what time did the motorist leave town B?
   At 9:30am

For how long was the motorist at B?
   For 30minutes or ½hr

c. What was the motorist's speed between town A and B?
   Solution
   $S = \dfrac{D}{T}$
   = 60KM ÷1 ½ HRS
   = 60km ÷3/2hrs
   = 60km x 2/3 hrs
   = $\dfrac{20km \times 2}{1hr}$

= 40km/hr

d. Calculate the motorist's total distance for the whole journey.
     100km + 100km
     200km

f. What was the total rest time?
     30min + 30min
     60minutes = 1hr

g. Find the motorist's average speed for the whole journey.
     A.S = TD
              TT
         = 200km
             5hrs
         = 40km/hr

3.   Find the motorist's average speed of the whole journey while traveling
         Total distance = 200km
         Total time = 4hrs
         Average speed while travelling = 200km
                                                        4hrs
                                                   = 50km/hr

DRAWING TRAVEL GRAPHS

1.   A Bus left x and 7:00am for town y, it travelled for 2hrs at an average speed of 40km/hr from x to y, it stayed at y for 30minutes before returning to x arriving at 12:00Noon. Draw a travel graph to show the movement of the bus.

Distance = S x T

          = 40km x 2hrs

                H
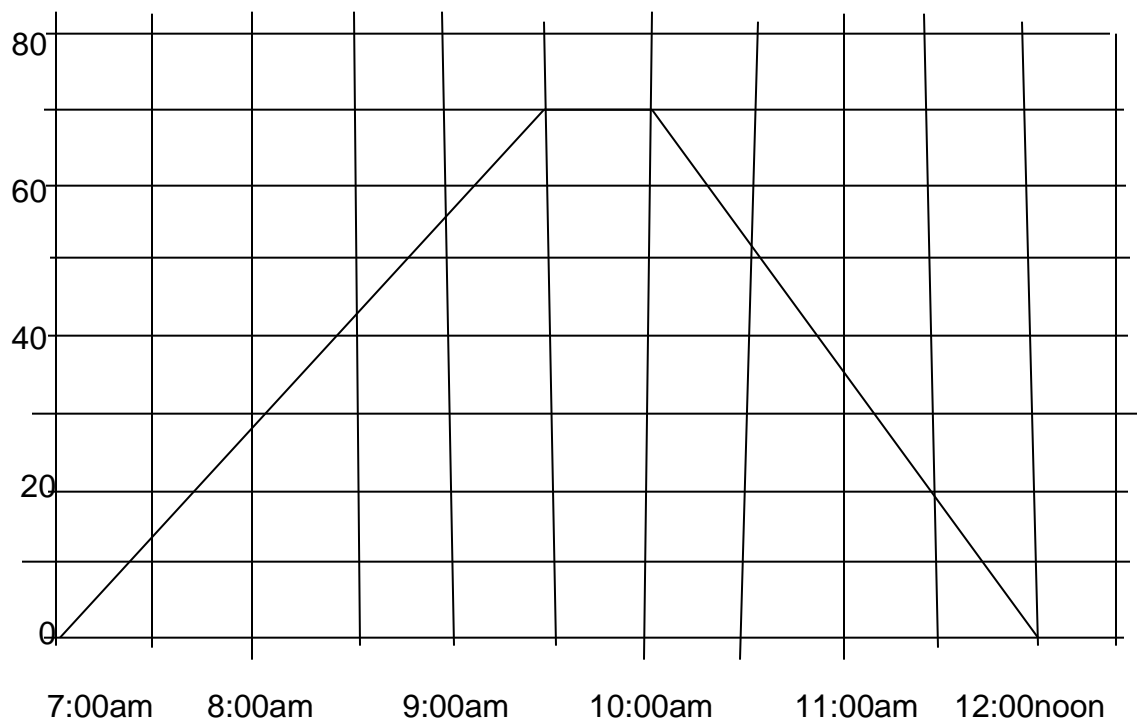
          = 80km

PIE CHARTS

1. The pie chart below represents Mugisha's monthly expenditure and saving. If he earns sh 72000;
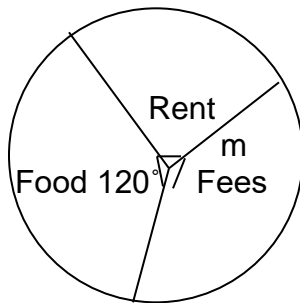
(a) How much does he spent on fees ?

Solution

M + 90 + 120 = 360˚

M + 210 = 360˚

M + 210 – 210 = 360˚ – 210˚

M = 150˚

Fees

150 x 72000/=

360˚

15 x 2000/=

30000/=

(b) What percentage of his salary is spent on food?

Solution

= 120 x 100%

  360

= 1 x 100%

  3

= 100%

  3

= 33 1%

    3

2. Kironde was given sh. 12000 for his pocket money and spent it as below .
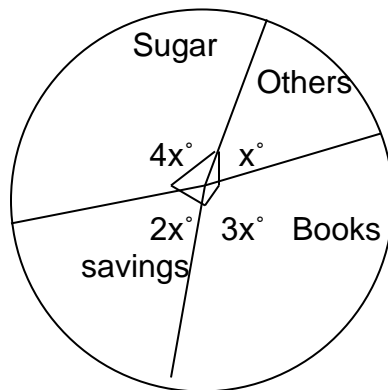
(a)   Find the value of x
      Solution
      4x + 3x + 2x + x = 360˚
      $\frac{10x}{10} = \frac{360˚}{10}$
      X = 36˚

(b)   How much does he save?
      Savings = 2x
               = 2 x 36˚
               = 72˚

               $= \frac{72 \times 12000/=}{360}$
               = 2 x 1200
               = 2400/=

(c)   How much does he spend on sugar than on books
Solution

Sugar = 4x	Books = 3x	Difference
= 4 x 36	= 3 x 36	= 144 – 108
= 144	**= 108**	**= 36**

$= \frac{36 \times 12000/=}{360}$
= 1200/= more

3. The pie chart below represents the expenditure of a family.
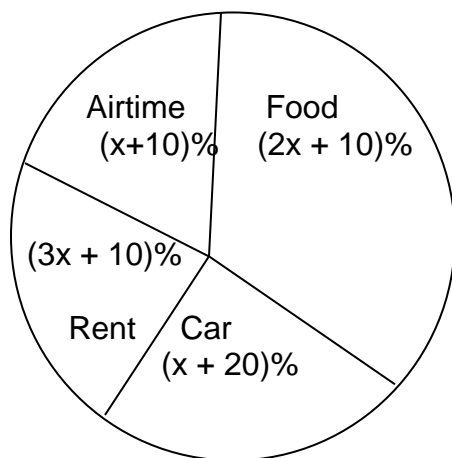
(a) Find the value of x.

x + 10 + 3x – 10 + x + 20 + 2x + 10 = 100%

x + 3x + x + 2x + 10 + 20 + 10 – 10 = 100%

7x + 30% = 100%

7x + 30 – 30 = 100% -30%

$\frac{7x}{7} = \frac{70\%}{7}$

x = 10%

(b) If the family spends sh 40000 more on car than on rent, find the family's total expenditure.

%ge of car	%ge of rent	difference in %ge
x + 20%	3x – 10%	320% - 20%
10% + 20%	3 x 10% - 10%	**10%**
10% + 30%	30% - 10%	
30%	**20%**	

Total expenditure % = 100%

10% represents sh. 40000/=

10% represents sh. $\frac{40000}{10}$

100% represents 100 x 4000/=

 400,000/=

DRAWING PIE CHARTS GIVEN FRACTIONS AND PERCENTAGES

1. Victor spends ¼ of his income on rent, 4/9 of the remainder on food and saves he rest.

(a) What fraction does he save?

Solution

Fraction for rent = ¼

Remaining fraction = $\frac{4}{4} - \frac{1}{4}$

$\frac{3}{4}$

Fraction for food = $\frac{4}{9} \times \frac{3}{4}$

$\frac{1}{3}$

Fraction for savings $= \frac{3}{3} - \frac{1}{3}$

$= \frac{9 - 4}{12}$

$= \frac{5}{12}$

(b) Using the above information, draw an accurate pie chart.
   Solution

Rent
$\frac{1}{4}$ x 360

90˚

food
$\frac{1}{3}$ x 360

120˚

savings
$\frac{5}{12}$ x 360

150˚
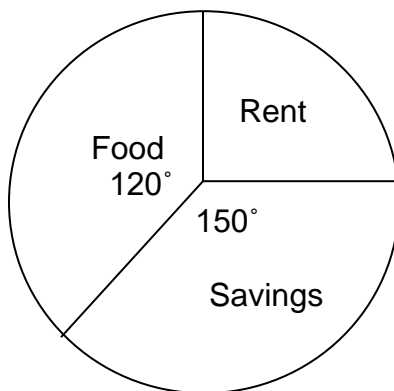
2. In a certain town, 40% of the population are Baganda, 10% are Basoga, 30% are Bagisu and the rest are acholi. Draw an accurate pie-chart for the above information.
   Solution

Baganda	Basoga	Bagisu	Acholi
$\frac{40}{100}$ x 360	$\frac{10}{100}$ x 360	$\frac{30}{100}$ x 360	360 – (144 + 36 + 108)
100	100	100	360 – 288
4 x 30	1 x 36	3 x 36	72˚
144˚	36˚	108˚	
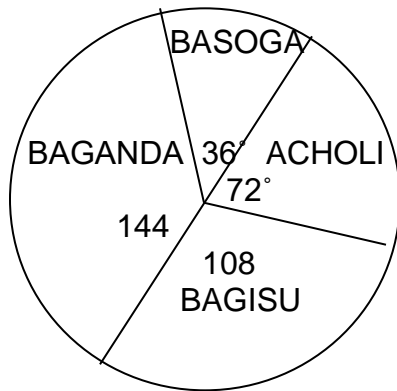
DRAWING PIE CHARTS GIVEN QUANTITIES

Nambooze spends her monthly salary as follows ;

sh. 12,000 on school fees

sh. 6000 on transport and

sh. 18,000 on food

Draw an accurate pie chart for this information

Total expenditure	Fees	Transport	Food
Sh. 12,000	$\underline{12000}$/= x 360	$\underline{6000}$/= x 360	$\underline{18000}$/= x 360
Sh. 6000	36000	36000	36000
Sh. 18000			
Sh. 36000	**120˚**	**60˚**	**180˚**
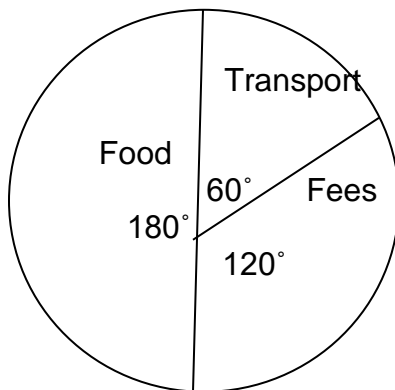
TEMPERATURE GRAPHS

The graph below represents the maximum temperatures of the week. Study it and use it to answer questions that follow
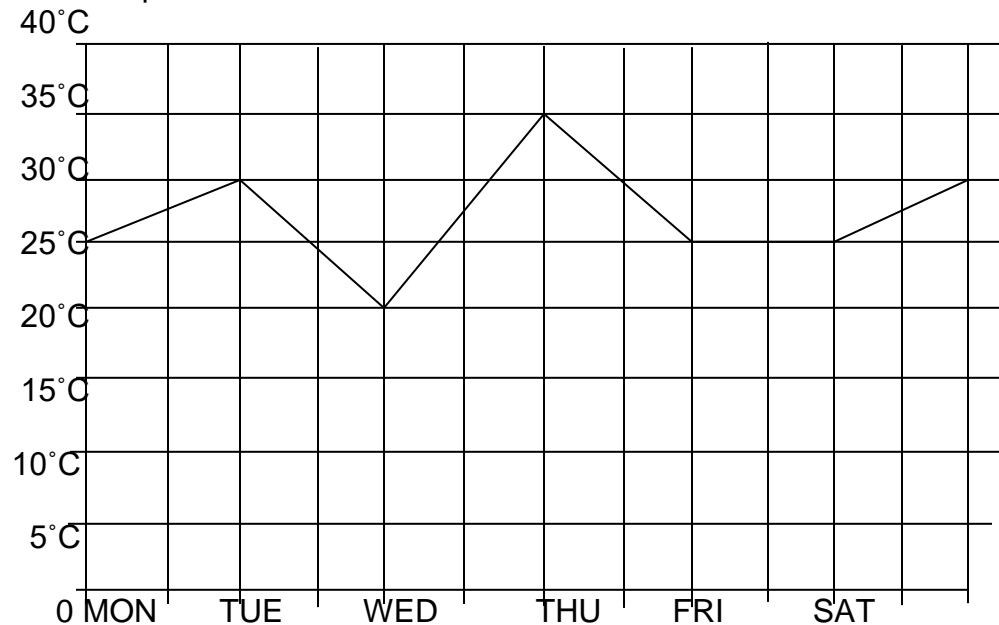
(a)   What was the highest temperature of the week?
        35⁰C

(b) Which day had the lowest temperature?
    Wednesday

(c) What was the drop in temperature between Tuesday and Wednesday?
    30˚C-20˚C=10˚C

(d) Calculate the average temperature for the whole week.
    $\frac{25 + 30 + 20\ 35 + 25 + 25 + 27.5}{7}$

    $\frac{190}{7}$

    $27\frac{1}{7}$˚C

APPLICATION OF MEAN

1. The mean age of 5 children is 12years, if a sixth child joins them, the mean age becomes 11years, find the age of the 6th child.
   Solution
   Total age of 5 children = 5 x 12
                   = 60yrs

   Total age of 6 children = 6 x 11
                   = 66yrs

Age of 6th child = (66 - 60) yrs
                                = **6yrs**

2. The average age of 6 boys is 13years. If one boy leaves the group, the average age becomes 14 years.
   Find the age of the sixth boy.

   Total age of 6boys = 6 x 13yrs
                              = **78yrs**

   Total age of 5boys = 5 x 14
                              = **70**

   Age of the 6th boy = (78 - 70)yrs
                              = **8yrs**

3. The average weight of 6pupils is 40kg; the average weight of other 4 pupils is 30kg. find the average weight of all the pupils
   Solution
   Total weight of 6 pupils = 6 x 40kg
                                   = **240kg**

   Total weight of 4 pupils = 4 x 30kg
                                   = **120kg**

   Total weight of 10 pupils = (120 + 240) kg
                                    = **360kg**

   Average weight of pupils = $\frac{360kg}{10}$
                                   = **36kg**

FORMING AND SOLVING EQUATIONS INVOLVING MEAN
1. The mean of y + 1, 5 and y is 6. Find the value of y.
   Solution
   $\frac{(y + 1) + 5 + y}{3} = 6$

   $\frac{Y + y + 5}{3} = 6$

   $3 \times \frac{2y + 6}{3} = 6 \times 3$

   $2y + 6 = 6 \times 3$
   $2y + 6 - 6 = 18 - 6$
   $\frac{2y}{2} = \frac{12}{2}$
   y = 6

2. The average of a, a-7, 3 and 2a is 8.
(a) Find the value of a.
   Solution
   $\dfrac{a + a + 3 + 2a + 3 - 7}{4} = 8 \times 4$

   $\dfrac{4 \times (a + a + 2a + 3 - 7)}{4} = 8 \times 6$

   $4a - 4 = 32$

   $4a - 4 + 4 = 32 + 4$

   $\dfrac{4a}{4} = \dfrac{36}{4}$

   a = 9

(b) Find the range
Solution
1) a = 9
2) a – 7 = 9 – 7
   = 2

3) 2a = 2 x a
   = 2 x 9
   = 18

4) 3

Range = 18 – 2
     = 16

PROBABILITY
Probability of success and failure.
1. The probability that peter will pass his examinations is 2/7. what is the probability that he will not pass his examinations?
   Solution
   $1 - \dfrac{2}{7}$

   $\dfrac{7}{7} - \dfrac{2}{7}$

   $\dfrac{5}{7}$

2. In a tin there are 30 blue and red pens. If the probability of picking a red pen is 3/5, how many red pens are in the tin?
   No of red pens = $\dfrac{3}{5}$ x 30
                   = 3 x 6
                   = 18

Probability when two teams play
In a football match a team will either win, draw or lose a game.
   a. What is the probability that a team wins the game?
  No of total chances = 3
  No of desired chances = 1
  Probability (win) 1
      3

b. Find the probability that a team draws the match.
  No of total chances = 3
  No of desired chances = 1
  Probability (draw) = 1
      3

c. What is the probability of a team losing a mach?

Tossing one coin.
If one coin is tossed, what is the probability of getting a head on top?
A coin has two sides the head (H) and the tail (T)
The head has the coat of arms
The tail is either a cow, fish or crane head.
Solution
Possible out comes = (H, T)
Number of possible out comes = 2
Expected out comes = (H)
Number of expected out comes = 1
Therefore probability = $\underline{n\ (E)}$
      n (D)
      ½

Tossing two coins.
If two coins are tossed once, what is the probability of two heads showing up?
    H   T

2nd H HH HT

Coin T TH TT

Total chances = (HH, HT, TH, TT)   Prob (HH) = No of desired chances
No of Total Chances = 4   N o of total chances
Desired chances = (HH)   = ¼
No of desired chances = 1

Tossing one die.
When a die is rolled once, what is the probability of getting an even number?
Total chances = (1, 2, 3, 4, 5, 6)
Number of total chances = 6
Desired chances = (2, 4, 6)
Number of desired chances = 3
Therefore probability = <u>No of desired chances</u>
                                    No of total chances
                          = <u>3</u> or <u>1</u>
                             6   2

Tossing two dice.
Calculate the probability of scoring a total of 8 when two dice are tossed at once

Die A	1	2	3	4	5	6
1	1, 1	1, 2	1, 3	1, 4	1, 5	1, 6
2	2,1	2,2	2,3	2,4	2,5	2,6
3	3,1	3,2	3,3	3,4	3,4	3,6
4	4, 1	4,2	4,3	4,4	4,5	4,6
5	5,1	5,2	5,3	5,4	5,5	6,6
6	6,1	6,2	6,3	6,4	6,5	6,6

Total chances = 36
Desired chances = 5
Probability = <u>5</u>
                   36

CIRCLES
Parts of a circle
1. Radius – line drawn from the centre to circumference.
2. Diameter – a line passing through the centre from circumference to circumference.
3. Arc – part of the circumference.
4. Circumference – distance round a circle.
5. Chord – straight line joining circumference to circumference.
6. Sector – an area of a circle bounded by two radii and arc.
7. Semi-circle – half a circle.
8. Quadrant – quarter circle.

RELATIONSHIP BETWEEN RADIUS AND DIAMETER
1. Find the diameter of a circle whose radius is

a) 10m   (b) 1 3/4m

      Solution   solution

Diameter = 2R   Diameter = 2R

    = 2 x R   = 2 x R

    = 2 x 10m   = 2 x 1 3/4m

    = 20m   = 2 x 7/4m

                                   = 3 ½m

2. Find the radius of a circle whose diameter is

a) 30cm   (b) 1 3/4 dm

R = $\underline{Diameter}$ R = D ÷ 2

     2   = 1 $\underline{3dm÷2}$

                                     4   1

$\underline{30cm}$ = $\underline{7dm}$ x ½

2   4

15cm   **= $\underline{7dm}$**

                                     8

CIRCUMFERENCE OF A CIRCLE
1.   Find the circumference of a circle whose diameter is

(a) 7cm.(use as 22/7)   (b) 10cm use ∏ as 3.14

TLD   C = TLD

$\underline{22}$ x 7cm   = 3.14 x 10cm

7   = $\underline{314}$ x 10cm

                                   100

= 22cm   = $\underline{314cm}$

                                   10

                              = 31.4 cm

2. Find the circumference of a circle whose radius is

(a) 7cm (use ∏= 22/7)   (b) (∏=3.14)

  C = 2TLR   C = 2TLR

  2 x $\underline{22}$ x 7cm   = 2 x $\underline{3.14}$ x 20m

    7   100

  = 44cm   = 2 x $\underline{314}$ x 20m

                                    100

                            = $\underline{628 \text{ x } 2m}$

                                  10

                          = $\underline{1256m}$

                                10

                        = 125.6m

FINDING RADIUS AND DIAMETER GIVEN CIRCUMFERENCE

1. The circumference of a circle is 44cm. Find the diameter of the circle.
(use ∏=22/7)

Solution

TLD = C

$\frac{22}{7}$D = 44cm

7 X $\frac{22D}{7}$ = 44cm x 7

$\frac{22D}{22}$ = $\frac{44cm}{22}$ x 7

D = 2cm x 7

D = 14cm

2. Calculate the radius of a circle whose circumference is 44m.
(use ∏ as 22/7)

Solution

2TLR = C

2 x $\frac{22}{7}$ x R = 44m

7 X $\frac{44R}{7}$ = 44m x 7

$\frac{44R}{44}$ = $\frac{44m}{44}$ x 7

R = 7m

FINDING NUMBER OF POLES AND SPACES

1. How many posts of 1.5m a part are needed to erect a circular hut of diameter 21m.

C = TLD

= $\frac{22}{7}$ x 21m

= 66m

No if posts = $\frac{66m}{1.5m}$

= 66 ÷ $\frac{15}{10}$

= 66 x $\frac{10}{15}$

66 x $\frac{10}{15}$

22 x 2

= 44posts

2. 11 Posts were fixed a distance of 4 meters a part to make a circular fence.

(a) Calculate the total distance a round the fence.

Solution

No of spaces = 11

Total distance = 11 x 4m

= 44m

(b) calculate the radius of the fence.

Solution

2TLR = C

2 x $\underline{22}$ x R = 44m
7

7 x $\underline{44R}$ = 44m x 7
7

$\underline{44R}$ = $\underline{44m \ x \ 7}$
44 44

R = 7m

APPLICATION OF CRIRUCMUFRERENCE (REVOLUTIONS)

Finding distance covered by circular objects in given number of revolutions.

1. A wheel is 35cm in diameter. What distance does it cover in
a) One complete revolution?

Distance /Length
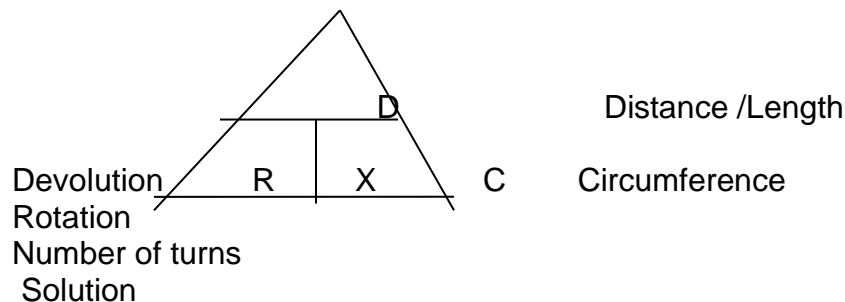
Devolution R X C Circumference
Rotation
Number of turns
 Solution
Distance = Circumference x Revolution
But circumference = TLD
= $\underline{22}$ x 35cm
7
= 22 x 5cm
**= 110cm**

Distance = 110cm x 1 Revol
= 110cm
b) 50 complete revolutions
**Solution**
Circumference = TLD No Distance = C x Revolution
= $\underline{22}$ x 35cm = 110cm x 50
7
**= 110cm** **= 5500cm**

Finding number of revolutions.
Revolutions = $\underline{Distance}$
Circumference

2. How many revolutions does a wheel of diameter 56cm make to cover a distance of 1760cm? (TL = $\underline{22}$)
7
Solution

No of rev.   =Distance
                    Circumference
But circumference = TLD
                    = $\frac{22}{7}$ x 56cm

                    = 22 x 8cm
                    = 176cm

No of Rev   = $\frac{1760cm}{170cm}$

                    = 10 Revolutions

FINDING DIAMETER/RADIUS
3. The length of a wire is 176m. if the wire is wound around a cylindrical tin 4 times, find the diameter of the tin. (use Tl = $\frac{22}{7}$)

Solution
Circumference = $\frac{Length\ of\ wire}{No\ of\ times}$

                    = $\frac{176m}{4}$

                    = 44mm
TLD = C
22D = 44m
7 x $\frac{22D}{7}$ = 44m x 7

$\frac{22D}{22}$ = $\frac{44m}{22}$ x 7
D = 14m

FINDING LENGTH OF ARCS OF SEMI CIRCLES AND PERIMETER OF SEMI CIRCLES
Length of arc = ½ TLD
1. Find the length of the arc of the semicircle below.

                    14m
Solution
Length of arc = ½ TLD
                    = ½ x $\frac{22}{7}$ x 14m

                    = 11 x 2m
                    = 22m

2. What is the distance around the semi-circle below (use TL = <u>22</u>)

Perimeter = (½ TLD) + D
    = (½ x <u>22</u> x 7m) + 7m
           7
    = 11m + 7m
    = 18m

LENGTH OF ARC AND PERIMETER OF QUADRANTS

Length of arc = ¼ 2TIR
1. Find the length of the arc of the figure below.

            Length of arc = ¼ x 2 TLR

14m

         = ¼ x <u>22</u> x 14mx2
              7
         = 11 x 2
         = 22m
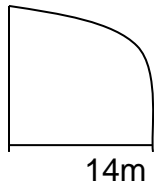
Perimeter of a quadrant = (¼ x 2TLR + 2R)
                =(¼ X 2 x <u>22</u> x 14)+(2x14m)
                       7

2. Calculate the distance around the figure below.
(USE TL as <u>22</u>)
      7

7m

    Perimeter = (¼ x 2TLR) + 2R
        = ¼ x 2 x <u>22</u> x 7) + (2 x 7m)
               7
      = 11m + 14m
      = 25m
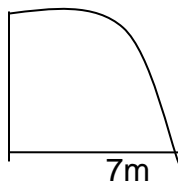
DISTANCE ROUND COMBINED SHAPES
  1.

28m

14m   ½ TLD

SOLUTION
  Length of arc = ½ TLD
      = ½ x <u>22</u> x 14m

$$7$$
= 22m
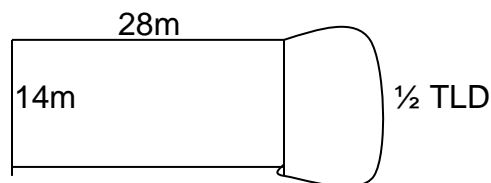
Perimeter = 22m + 28m + 14m + 25m

= (50 + 42) m

= 92m

2. Find the distance around the shaded part .

Solution
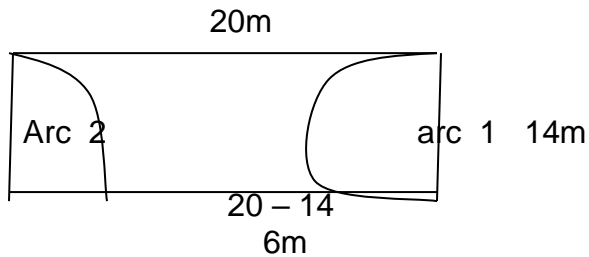
20m

Arc 2   arc 1   14m

20 – 14

6m

Length of arc	Arc 2	
½ TLD	¼ x 2TLR	Perimeter
½ x $\frac{22}{7}$ x 14m	¼ x 2 x $\frac{22}{7}$ x 14m	22m + 22m + 20m + 6m
		44m + 26m
22m	**22m**	**70m**

AREA OF A CIRCLE

Area of a circle $= TLR^2$

1. Calculate the area of a circle whose radius is 7m.

(Use TL as $\frac{22}{7}$)

Area $= TLR^2$

$= \frac{22}{7}$ x 7m x 7m

$= 154m^2$

2. Find the area of a circle whose diameter is 28cm.

(Use TL $= \frac{22}{7}$)

Solution

Area   = TLR

$= \frac{22}{7}$ X $\frac{28cm}{2}$ x $\frac{28cm}{2}$

= 22 x 14cm x 2cm

= 22 x 28cm²

$= 616cm^2$

FINDING AREA OF A CIRCLE GIVEN CIRCUMFERENCE

1. calculate the area of a circle whose circumference is 44dm.

(Use TI $= \frac{22}{}$)

7
Procedure
i.   Use given circumference to find radius
        2TLR= C
ii.   Use the radius to find area
        Area = TLR²

Solution
Radius of the circle   **Area of circle**
Area   2TLR = C
          7   Area = TLR²
       2 x 22 x R = 44dm
            7   = 22 x 7dm x 7dm
       7 x 44 x R   = 44dm x 7   7
            7   = 22dm x 7dm
       44R = 44dm X 7   **= 154dm²**
       44   44
       R = 7dm

FINDING RADIUS OF A CIRCLE GIVEN AREA
Find the radius of circle whose area is 154m².
(Use TL = 22)
          7
Solution
TLR² = Area
22 x R² = 154m
7
7 x 22R² = 154m x 7
      7   22

√R² = √49m²
R = 7m
FINDING CIRCUMFERENCE WHEN AREA IS GIVEN
STEPS TAKEN
1. Use the given area to find radius
    TLR² = AREA

2. Use the radius to find circumference
    C = 2TLR

Question
The area of a circle is 154cm². Find the circumference of the circle .
(Use TL as 22)
          7
Solution
Radius of the circle   circumference
TLR² = Area   C = 2TLR

$\frac{22R^2}{7} = 154cm^2$ $\qquad\qquad = 2 \times \frac{22}{7} \times 7cm$

$7 \times \frac{22R^2}{7} = 154cm \times 7$ $\qquad\qquad$ **= 44cm**

$\sqrt{R^2} = \sqrt{49cm^2}$

R = 7cm

FINDING AREA OF SEMI-CIRCLES

1. Find the area of a semi circle whose radius is 21dm.
   (Use TL as $\frac{22}{7}$)

   Solution
   Area $= \frac{1}{2} TLR^2$
   $= \frac{1}{2} \times \frac{22}{7} \times 21m \times 21m$
   $= 11 \times 16m^2$
   $= 693m^2$

2. Calculate the area of the semi-circle below
   (Use TL $= \frac{22}{7}$)

   14m
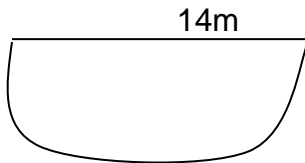
   Area $= \frac{1}{2} TLR^2$
   $= \frac{1}{2} \times \frac{22}{7} \times 14m \times 14m$
   = 77m²

FINDING AREA OF QUADRANTS
Calculate the area of the quadrant below
(Use TL $= \frac{22}{7}$)

7m
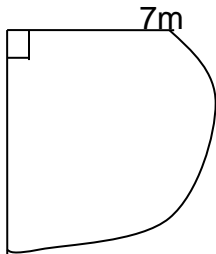
Area $= \frac{1}{4} \times TLR^2$
$= \frac{1}{4} \times \frac{22}{7} \times 7m \times 7m$
$= \frac{77}{2}m$
= 38½m²

AREA OF OTHER SECTORS
Find the area of the sector below
(Use TL $= \frac{22}{7}$)

Area $= \frac{120}{360} \times TLR$

120
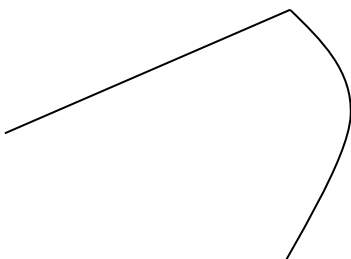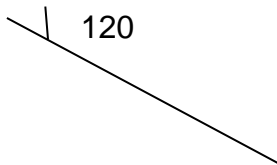
$$= \frac{1}{3} \times \frac{22}{7} \times 21cm \times 21cm$$
$$= 22 \times 21cm^2$$
$$\underline{\textbf{= 462cm}^2}$$

AREA OF COMBINED SHAPES

20m

14m
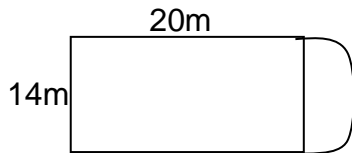
Area of rectangle   Area of semicil   Total area
L x W   ½ x $\frac{22}{7}$ x $\frac{14}{7}$ x $\frac{14}{7}$ 280m²
20m x 14m   + 77m²
280m²   77m $\underline{357m^2}$

AREA OF SHADED PORTIONS
1. Find the area of the shaded region

15m

16m
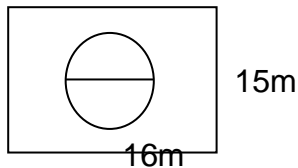
Area of whole figure   Area un shaded   Area shaded
Area = L x W   Area = TLR²   Area = 240m
    = 16m x 15m   = $\frac{22}{7}$ x $\frac{14m}{7}$ x $\frac{14m}{7}$ = 154m²
    =240m²   **86m²**
        = 154m²

2. Find the area of the shaded portion
(use TI $=\frac{22}{7}$)

MORE ABOUT AREA
1. A rectangular floor measures 400cm by 300cm.
How many square tiles 50cm by 50cm are required to cover the floor?
Solution
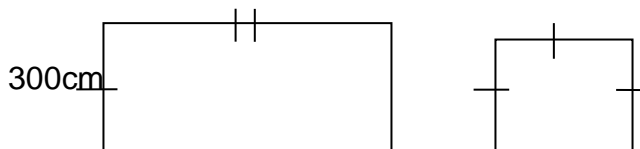
300cm

```
        ||                          |
      400cm                        50cm
```

No of tiles = (L) X (W)
                   S   S
= $\frac{400cm}{50cm}$ x $\frac{300cm}{50cm}$
=   8 x 6
=   ***48 tiles***

2. Abdul cut out circular plates of diameter 7cm from a rechangular. Sheet of metal of length 45cm and width 35cm
(Use TL= $\frac{22}{7}$)

a) How many circular plate did he cut out
      Solution
      No of circular plates   = $\frac{(L)}{D}$ X $\frac{(W)}{D}$
= $\frac{45cm}{7cm}$ x $\frac{35cm}{7cm}$
= 6 x 5
= 30 plates

b) Find the area of the un used sheet after cutting out the circular plates.
Solution

Area Circular	Area of 30 Plates	Area Un Used
A = L x w	A = TLr² x 30	1575cm²
45cm x 35cm	= $\frac{22}{7}$ x $\frac{70cm}{2}$ x $\frac{7cm}{9}$ x 50cm	- 1155cm²
1575cm²	= 11 x 7cm² x 15	**420cm²**
	= 1155cm²	

PACKING CURE AND CUBOIDS IN BOXES

1. a box measures 24cm by 30cm and height of 35cm
(a) How many cubes of sides 4cm can fit into the box
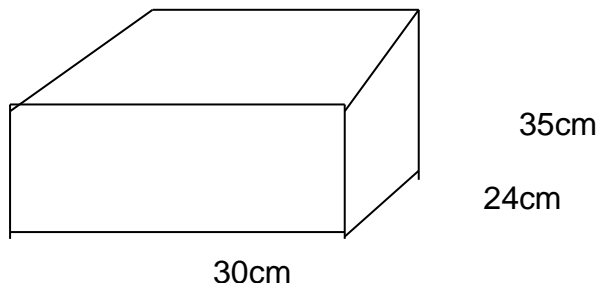
35cm

24cm

30cm

No of cubes = L X W X h

$$= \frac{30cm}{4cm} \times \frac{24cm}{4cm} \times \frac{35cm}{4cm}$$

=   7 x 6 x 8

=   336 cubes

(b) Find the space left empty after packing all the cubes in the box.
Solution

Volume of big box	**Volume of 336cubes**	**Space left**
Vol = L x W x h	Vol = S x S x S x 336	252400cm³
= 30cm x 24cm x 35cm	= 4cm x 4cm x 4cm x 336	- 21504cm³
= 720cm x 35cm	= 64cm x 336	
3696cm³		
= 25200cm	**= 21504cm³**	

PACKING TINS IN BOXES AND FINDING SPACE LEFT

1. How many tins (B) type can fit in Box (A)

8cm   56cm

35cm

42cm

7cm
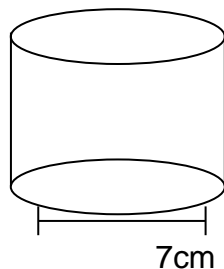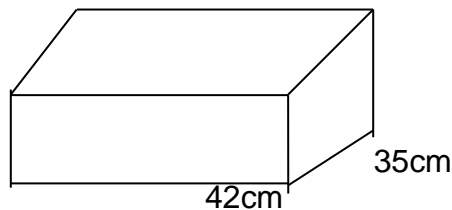
No of tins   = $\frac{(L)}{D}$ X $\frac{(W)}{D}$ X $\frac{(H)}{h}$

$$= \frac{(42cm)}{7cm} \times \frac{(35cm)}{7cm} \times \frac{(56cm)}{8cm}$$

= 6 x 5 x 7

= 30 x 7

    = 210 tins

2. Calculate the space left when tins (X) are packed in box (V)
(Use TI = $\frac{22}{7}$)

14cm   30cm

X
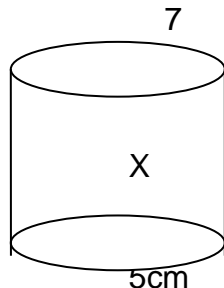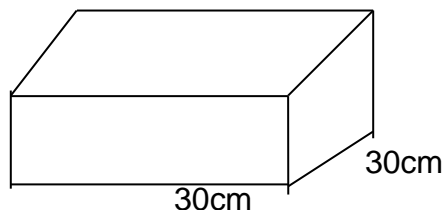
30cm

5cm   30cm

No of tins that fit in the box = ($\underline{S}$) X ($\underline{S}$) X ($\underline{S}$)
                                                   D   D   N

= $\underline{(30cm)}$ x $\underline{(30cm)}$ x $\underline{(30cm)}$
      5cm   5cm   14

= 6 x 6 x 2

= 36 x2

= 72 tins

Vol. of box   = S x S x S

= 30cm X 30cm X 30cm

= 900cm² x 30cm

= 27000cm³

Vol. of 72 tins   = TLR² X 72

= $\underline{22}$ X $\underline{5cm}$ x $\underline{5cm}$ x 14cm x 72
     7   2   2

= 11 x 5cm x 5cm² x 72

= 55cm x 5cm x 72

= 275cm³ x 72

= 19800cm²

FINDING VOLUME OF A CYLINDER

1. A cylindrical tin has radius of 7cm and height of 10cm.
       Calculate its volume

Solution

Vol= TLR²h

= $\underline{22}$ x 7cm x 7cm x 10cm
     7

= 22cm x 70cm²

= 1540cm³

2. calculate the volume of a cylindrical tin whose height is 5cm and a diameter of 10cm
       (Use TL = 3.14)

Solution

Vol   = TLR²h

= 3.14 x $\underline{10cm}$ x $\underline{10cm}$ x 5cm
             2   2

= $\underline{3.14}$ x 5cm x 5cm x 5cm
    100

= $\underline{(157 \text{ x } 5)}$ cm³
        2

= $\underline{785cm³}$
     2

= 392½cm³

HOW TO FIND HEIGHT OR RADIUS WHEN VOLUME IS GIVEN

1. Calculate the height of a cylinder whose volume is 1694m³, if a cylinder has a radius of 7m.

   Solution

   TLR^2h = vol

   $\dfrac{22 \times 7cm \times 7cm \times h}{7}$ = 1694cm³

   $\dfrac{22 \times 1cm \times 7cm \times h}{22 \times m \times 7m}$ = $\dfrac{1694m \times m \times m}{22 \times m \times 7m}$

   h = 11m

2. Find the radius of a cylinder whose volume is 62.8cm and height 5cm.

   (Use TL = 3.14)

   Solution

   $TLRh$ = Vol.

   3.14 x R x 5cm = 62.8cm

   $\dfrac{314 \times 5 \times R}{100}$ = $\dfrac{628cm}{10}$

   $\dfrac{1570cm \times R}{100}$ = $\dfrac{628cm}{10}$

   10 x $\dfrac{157cm}{10}$ x R = $\dfrac{628cm}{10}$ x 10

   $\dfrac{157cm \times R}{157cm}$ = $\dfrac{628cm}{157cm}$

   R = $\dfrac{628 \times cm \times cm \times cm \times cm}{157 \times cm}$

   R = 4cm

   R = 2cm

SUBTRACTION OF VOLUME

1. The figure shows a cylindrical hollow pipe. Find the volume of the pipe.

   (Use TL = $\dfrac{22}{7}$)

   Solution
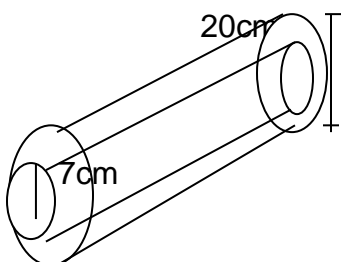
   Vol. of whole figure (outer cylinder)

   Vol. = TLR^2h

   = $\dfrac{22}{7}$ x $\dfrac{14cm}{2}$ x $\dfrac{14cm}{2}$ x 20cm

   = 22 x 7cm² x 20cm

   = 154cm² x 20cm

   = **3080cm²**

   Vol. of hollow (inner cylinder)

Vol = TLR²h

= $\frac{22}{7}$ x $\frac{7cm}{2}$ x $\frac{7cm}{2}$ x 20cm

= 11 x 1cm x 7cm x 10cm

= 770cm³

Vol of the pipe

  3080cm³

- 770cm³

 2310cm³

2. Below is a cylindrical piece of wood after frilling a hollow in it.
(Use TL = $\frac{31}{7}$)

8cm   21cm

10cm
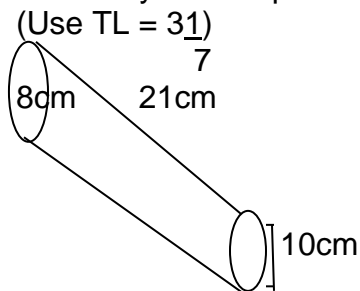
(i)   Find the volume of the materials removed to drill the hollow.
Solution

Vol = THR²h

= $\frac{22}{7}$ x $\frac{8cm}{2}$ x $\frac{8cm}{2}$ x 21cm

= 22 x 4cm x 4cm x 3cm

= 22 x 48cm³

= 1056cm³

(ii)   What is the volume of the wooden cylinder left after drilling the hollow?
Solution

Vol of the whole wood   = TLR²h

= $\frac{22}{7}$ x $\frac{10cm}{2}$ x $\frac{10cm}{2}$ x 21cm

= 22 x 5cm x 5cm x 3cm

= 22 x 75cm³

= 1650cm³

Vol of wood left   1650cm³

- 1056cm³

   1650cm³

COMPARING VOLUMES

1. the figures below have the same volume

A

7cm

B   4cm
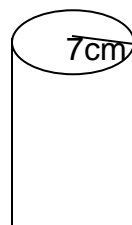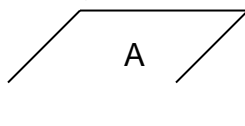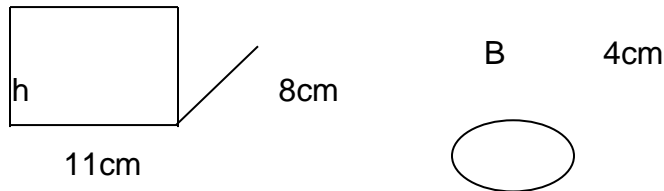
(a) Find the height of A.
Solution

Vol. of B	Height of A
Vol. = TLR²h	L x W x h = Vol.
$\frac{22}{7}$ x 7cm x 7cm x 4cm	11cm x 8cm x h = 616cm (same Vol as B)
22cm x 7cm x 4cm	$\frac{28cm \times 8cm \times h}{11cm \times 8cm}$ = $\frac{616cm \times cm \times cm}{11cm \times 8cm}$
154cm² x 4cm	**h = 7cm**
616cm³	

2. A cylindrical tank full of water has a diameter of 28m and height of 20metres. Find the height of water which remains after removing 154m of water.
Solution

Volume of tant who full   Vol of water that remains

Vol.   = TLR²h   12320m³

        = $\frac{22}{7}$ x $\frac{8cm}{2}$ x $\frac{28m}{2}$ x 20m   - 1540m³

                                       10780m³

       = 22 x 14m x 2m x 20m

       = 308m 40m

       = 12320m

Height of water left

TLRh   = Vol of water left

$\frac{22}{7}$ x $\frac{28m}{2}$ x $\frac{28m}{2}$ x h = 10780m

$\frac{22 \times 14m \times 2m \times h}{22 \times 14m \times 2m}$ = $\frac{10780m \times m \times m}{22 \times 4m \times 2m}$

h = 17½m

METHOD II

Height of the tank = 20m

Height of the water removed

TLRh =Vol.

$\frac{22}{7}$ x $\frac{28m}{2}$ x $\frac{28m}{2}$ x h = 1540m

$\frac{22 \times 2m \times 14m \times h}{22 \times 2m \times 14m}$ = $\frac{1540m}{22 \times 2m \times 14m}$

h = $\frac{5m}{2}$

h = 2 ½ m

Height of water which remains = 20m -2 ½ m

= 20 – 5

= 1   2

= $\frac{40m – 5m}{2}$

= $\frac{35m}{2}$

= **17 ½ m**

VOLUME IN LITRES
1. calculate the volume of the figure below in Litres
   Solution
   1 liter = 1000cc
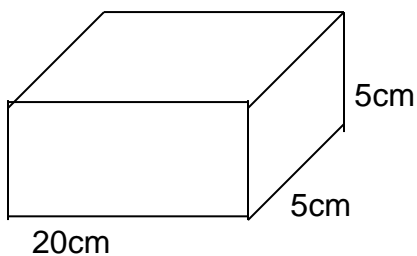
5cm
5cm
20cm

Vol m.c.c   = L x W x h

= 20cm 5cm x 5cm

= 100cm x 5cm

= **500cm³**

Vol. in litres
IL = 1000cm
1000cm = IL
1cm = $\frac{1}{1000}$ L
500cm = 500 x $\frac{1}{1000}$ L

= $\frac{5 L}{10}$

= **0.5L**

2. The tin below holds 2 Litres when completely filled with water. Find h.
Change 2c to cm³
1L = 1000cm³
2L = 2 x 1000cm³
= 2000cm³
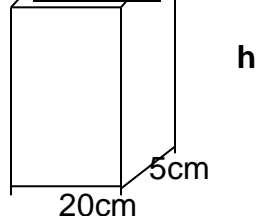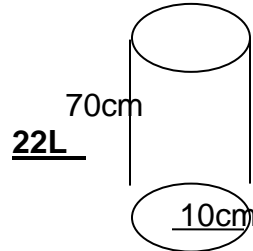
h
5cm
20cm

L x W x h   = Vol
20cm x 5cm h   200cm³
20 x 5cm   20cm x 5cm
2000cm x cm x cm
20cm x 5cm
h = 20cm

3. Nanfuka filled a cylindrical tin whose radius is 10cm and height 70cm with passion juice. If she sells it at sh 600 per litre, how much money will she get after selling all the juice.
   Solution

Vol. in cc
Vol = TLR²h
= $\frac{22}{7}$ x 10cm x 10cm x 7cm

= 22 x 10cm x 10cm x 10m
= **22000cm²**

70cm

22L

10cm

Vol. in litres
22000cc = $\frac{22000cc \times IL}{1000cc}$
=

The cost of 22L
IL costs 600/=
22L cost 22 x 600/=
      13200/=

TOTAL SURFACE AREA OF ACYLINDER
1. Calculate the surface area of the cylinder below.

Solution
T.S.A = TLR² + 2TLRh + TLR²
= ($\frac{22}{7}$ x $\frac{14cm}{2}$ x $\frac{14cm}{2}$) + (2 x $\frac{22}{7}$ x $\frac{14cm}{2}$) x 10cm + ($\frac{22}{7}$ x $\frac{14cm}{2}$ x $\frac{14cm}{2}$)

= 22 x 7cm² + 2 x 22cm x 10cm + 22 x 7cm²
= 154cm² + 440cm² + 154cm²
= **748cm²**

2. The diagram below shows a cylindrical tin without the top cover calculate its surface area.

T.S.A = $\frac{22}{7}$ X $\frac{7cm}{2}$ x $\frac{7cm}{2}$ + 2 x $\frac{22}{2}$ x $\frac{7cm}{2}$ x 7cm

  = $\frac{77cm^2}{2}$ + 154cm²

  = 38 ½ cm² + 154cm

  = **192½ cm²**

3. Calculate the surface area of a hollow cylinder of radius 7cm and height 5cm. (Use TL = $\frac{22}{7}$)

T.S.A = $\frac{2 \times 22 \times 7cm \times 5cm}{7}$

  = 44cm x 5cm

  = **220cm²**

MORE ABOUT VOLUME AND SURFACE ARAE OF ACYLINDER

1. A welder was given a metal sheet with measurements as shown in the diagram below. He welded it into a hollow cylinder making the height 1000cm.
   (Use TL = $\frac{22}{7}$)

   44ocm

   100cm
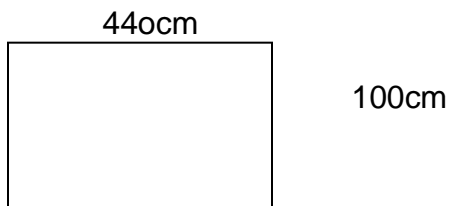
(a) What is the surface of the metal needed to cover the bottom of the cylinder?

Radius

2THR   = C

2 x $\frac{22}{7}$ x R = 440cm

7 x 44R = 440cm x 7

$\frac{44R}{44}$ = $\frac{440cm \times 7}{44}$

R = 70cm

Area of metal needed to cover the bottom

Area TLR

$\frac{22 \times 70cm \times 70cm}{7}$

22 x 700cm

154cm

Calculate the maximum volume of water the cylinder will hold.

Solution

Vol. in cc   = TLR²h   Vol. in litres

= 22 x 70cm x 70cm x 100cm   1000cm =IL
     7   1540cm = 1540000
= 22 x 70cm x 1000cm²   1000cm
= **1540000cm**   **= 1540Litres**

A TRIANGULAR PRISM.
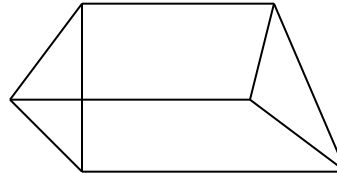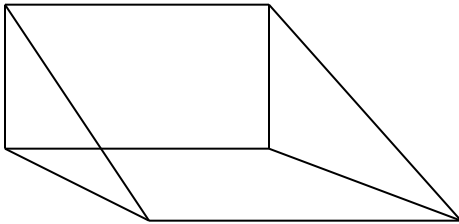
A triangular prism has a total of 5 faces.
Two faces of the triangular prism are triangular and three faces are rectangular.
It has 9 edges
It has got 6 vertices

VOLUME OF TRIANGULAR PRISM
Vol. = Area of△   length of prism

Calculate the volume of the figure below.
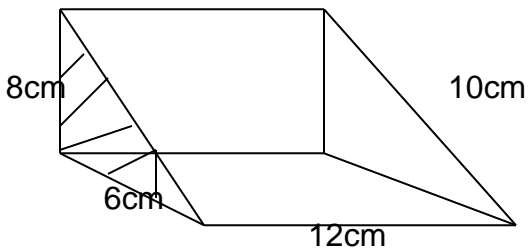
8cm   10cm

6cm
        12cm
Vol.   = Area of D x L
      = (½ b x h) x L
      = ½ x 6cm x 8cm x 12cm
      = 3cm x 8cm x 12cm
      = 24cm² x 12cm²
      = **288cm³**

What is the volume of the prism below?
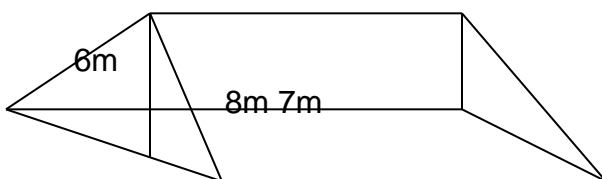
6m

    8m 7m

5m

10m

Vol   =Area of D x length

= ½ x b x l x l

= ½ x 5m x 8m x 10m

= 5m x 4m x 10m

= 20m² x 10m

= **200m²**

FINDING LENGTH,HEIGTHT OR BASE OF THE TRIANGULAR PPRISM GIVEN THE VOLUME.

1. The volume of the triangular prism below is 700cm.
Find L.

L

7cm

8cm

10cm

Area of D x L   = Vol.

½ x b x h x L = 700cm²

½ 10cm x 7cm x L = 700cm³
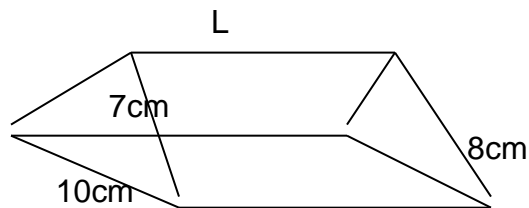
35cm x L = 700cm³

35cm = 700cm³
35cm   35cm

L = 700cm x cm x cm
     35cm x cm

L = 20cm

2. Below is a triangular prism whose volume is 480m
Find h.

h

6m

20m

Area of D x L   = Vol.

½ x b x h x L   = 480m³
½ x 6m x h x 20m   = 480m³
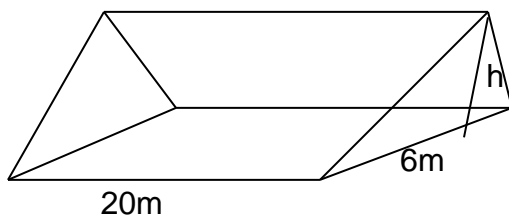
$\underline{3m \times 20m \times h} \qquad \qquad = \underline{480m \times m \times m}$
3m x 20m   3m x 20m

h = 8m

APPLICATION OF PYTHAGORAS THEOREM ON TRIANGULAR PRISM.
A. Use the figure below to answer questions that follow.
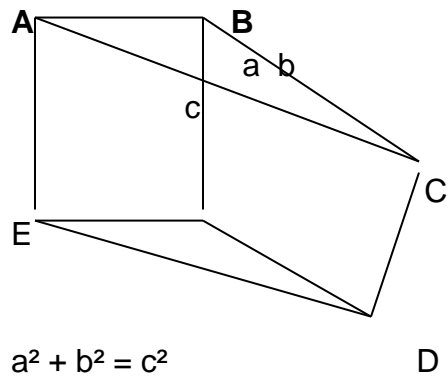
a² + b² = c²   D
a² + (6m)² = (10m)²
a² + 6m x 6m = 10m x 10m
a² + 36m = 100m²
a² + 36m² – 36m² = 100m² – 36m²
a² = 64m²
a² = 8m
AB = 8m

B.   Find the volume of the prism.
Vol = Area of D x L
    = ½ x b x h x L
    = ½ x 8m x 6m x 12m
    = 4m x 6m x 12m
    = 24m² x 12m
    = 288m²

4cm

10cm

Solution

3cm   3cm   5   4cm   3cm
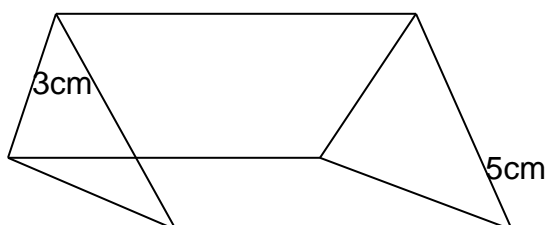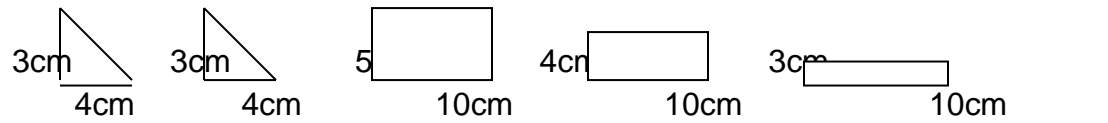
4cm   4cm   10cm   10cm   10cm

= (½ x 3cm x 4cm) x 2 + (5cm x 10cm) + (10cm x 4cm) + (10cxm x 3cm)

= 12cm² + 50cm² + 40cm² + 30cm²

= **132cm²**

Find the total surface area of the figure below,

13m

h

10m

20m
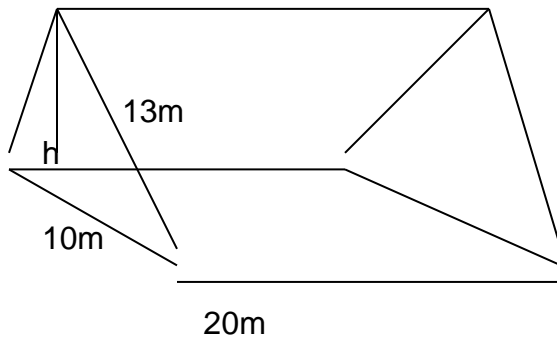
Solution

Value of h

6 + 6 = c

h + (5m) = (13m)

h + (5m x 5m) =13m + 13m

h + 25m = 169m

h + 25m – 25m = 169m -25m

h = 144m

h = 12m

Surface area

12m   12m
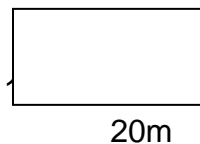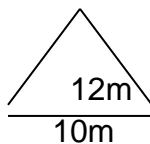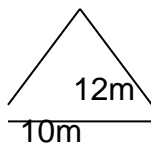
10m   10m   20m   20m

= (½ x 10m x 12m x 2) + (20m x 13m) + (20m x 13m) + (20m x 10m)

= 120m² + 260m² + 260m² + 200m²

= **840m²**

VOLUME OF THETRAPEZOIDAL PRISM.
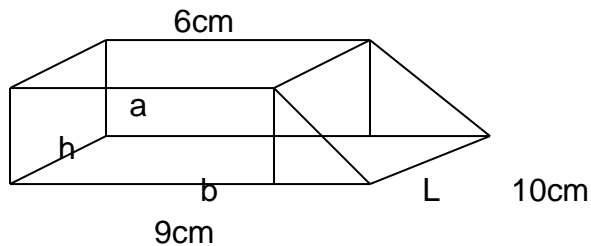
Vol = ½ h (a + b) x length
½ x 4cm (6cm + 9cm) x 10cm
2cm x 15cm x 10cm
30cm x 10cxm
300cm

SPEED ,TIMEAND DISTANCE.
AVERAGE SPEED
Average speed = total distance
                        Total time.

A man covered 50km in2hours and another 5okm in 3hours.
Find his average speed for the whole journey.

Total distance = 50km + 50km
              = 10km
Total time = 2hours + 3hours
          = 5hours

Average speed = 100km
                  5hrs
            = 20km/hr

Calculate the average speed of a motorist who rode from X to YAT 60KM/hr for 3hr and
continued to Z at 40km/hr for another 3hrs.

Solution
Distance from x to y   = 60km x 3hr

Hr

= 180km

Distance from y to z at 40km/hr for 3hrs = $\frac{40km \times 3hrs}{hr}$

= **180km**

Total distance from x to z   = 180km + 120km

= **300km**

Total time   = 3hrs + 3hrs

= **6hrs**

Average speed   = $\frac{300km}{6hrs}$

= **50km/hr**

3.Nyangweso drove a distance of 40km at a speed of 20km/hr. Due to the bad road ,he show down speed to 15km /hr to cover 45km . Find the average speed for the whole journey.

Time taken at 20km/hr = $\frac{40km/hr}{20km}$

= 2hrs

Time taken at 15km/hr   = $\frac{45km}{15km/hr}$

= 3hrs

Total distance covered   = 40km +45km

= 85km

Total time taken   = 2hrs + 3hrs

= 5hrs

Average speed   = $\frac{total\ distance}{Total\ time}$

= $\frac{85km}{5hrs}$

= 17km/hr

AVERAGE SPEED OF RETURN JOURNEYS

1.Lubwama drove at 55km/hr for 4 hours .if he returned following the same road at 11okm/hr, find his average speed for the whole journey.

Distance covered = 220km + 220km
= 440km

Total time taken = 4hrs + 2hrs
= 6hrs

Average speed = 440km
6hrs
= 73 2/6km/hr
= 73 1/3km/hrs

A and B are two towns a part. Lunyolo drove from A to B at 40km/hr and then returned to A though the same route at 60km/hr. calculate LAunyolo average speed for the whole journey.

Total taken to cover 80km at 40km/hr = 80km/hr
40km
= 2hrs

Time taken to cover at 60km/hr = 80km/hr
60km/hr
= 1 1/3 km/hrs

Total distance from A and B and back = 80km + 50km
= 160km
= 2hrs + 1 1/3hrs
= 3 1/3hrs.

Average speed = total distance
Total time

= 160km ÷ 3 1/3hrs

= 160km ÷ 10hrs
     3

= 160km x 3
    10hrs

= 16km x 3
   1m

= **48km/hr**

AVERAGE SPEED INVOLVING STOPPAGES /RESTS.

Kato left town A driving at75km/hr . After 2hrs, his car got a puncture and he delayed for 45minutes. He then continued at 60km/hr for 2hours and 15minutes to town B. What distance had kato covered before his car got a puncture.

Distance   = S x T

     = 75km x 2hrs
      hr

     = 75km x 2

     = 150km

How far is town B from town A.

Distance coved after puncture = S x T

          = 60km 2 15hrs
            Hr 60

          = 60km x 9
              4

          = 15km x 9

          = 135km

Total distance = 150km + 135km
     = 285km

CALCULATE KATO AVERAGE SPEED FOR WHOLE JOURNEY.

Solution

Total distance   = 285km

    = 2hrs + 45krs + 2 ¼ hrs
       60

    = 2hrs + ¾ hrs + 2 ¼ hrs

2hrs + 2hrs + ¾ hrs + ¼ hrs

4hrs + 1hr

5hrs

Average speed   = total distance

                 Total time

             = 285km

                 5hrs

             = 57km/hr

Town R and S are 120km a part . Okiror drove from R starting at 10:30am ,he arrived at S where he stayed for 1hr and then returned to R through the same road at a speed of 60km/hr.

(a)At what time did okiror arrived at R from S.

Solution

Time taken from R to S   = 120km/hr

                             60km

Time he left S = 10 30am

              + 1 00

              11: 30am

The time when he arrived at R   = 11:30am

                                 2:00

                               13:30

                       1:30pm

a)calculate okiror average speed for the whole journey.

Solution

Time taken from R to S   = 10:30am – 9:00am

                          Hrs   Min

                          10   30

```
                    - 9        00
                      1        30
```

= 1hrs 30 minutes

= 1 ½ hrs

Total time　　= 1 ½ hrs + 2hrs + 1hr

　　　　　　　= 4 ½ hrs

Total distance = 12okm + 120km

　　　　　= 240km

Average speed　　= total distance

　　　　　　　　　total time

　　　　　　= 240km ÷ 4 ½ hrs

　　　　　　= 240km ÷ 9/2hrs

　　　　　　= 240km x 2

　　　　　　　　　9h

　　　　　　= 4480km

　　　　　　　9hrs

　　　　　　= 53 1/3km/hr

c)calculate okiror average speed for the whole journey while travelling.

Total distance = 240km

Total time = 1 ½ hrs + 2hrs

　　　　= 3 ½ hrs

Average speed　　= 240km　　3 ½ hrs

　　　　　　　= 240km　　7/2 hrs

　　　　　　　= 240km 2/7hrs

　　　　　　　= 480km

　　　　　　　　7hrs

　　　　　　　= 684/7km/hr

TELEGRAMS

NOTE

1. A telegram is a written message .

2. In telegrams , punctuation marks eg. commas , full stops are counted as words.

3. figures eg 234 , 26 are also counted as words.

　　The cost of sending a telegram is sh.1500 for the first 10 words and sh.200 for each extra word. Find the cost the cost of sending a telegram having 27 words.

Total number of words = 27
1st ten words cost sh.   = 1500
Additional words   = 27 – 10
                = 17 words
Cost of 17 words   = 17 x 200/=
                = 3400/=

Total cost of 27words   = 1500/= + 3400/=
                = 4900/=

The cost of sending a telegram is sh.700 for the first 5 words , sh.400 for each of the next 5 words and sh. 100 for each additional word . Find the cost of the cost of sending the telegram below.

Solution
Total number of words   = 14
1st 5 words cost sh.   = 700
Remaining words   = 14 – 5
                = 9
Cost of next 5 words   =5 x 400/=
                = 2000/=

Remaining words   9– 5 = 4
Cost of 4 words   = 4 x 100/=
                = 400/=

Total cost of 14words   = 700/= + 200/= + 400/=
                = 3100/=

ANNOUNCEMENTS.
Note.
In announcement punctuation marks are not counted as words in telegrams.

1. The cost of sending a death announcement or radio Wolokoso is sh. 100 for the first 25 words. Find the cost of sending 2 death announcement of 55 words each.

1 announcement

Total number of words	= 55
Cost of 25 words	= 100/=
Remaining words	= 55 – 25
	= 30 words
Cost of 30 words	= 30 x 100/=
	= 3000/=

Total cost of 55 words = 3000/= + 100/=
$\qquad\qquad$ = 4000/=

Charge for 2 death announcements = 4000/= x 2
$\qquad\qquad\qquad\qquad$ = 8000/=

2. The cost of making an announcement on radio is a follows: for first the first 25 words sh. 1500.each additional word.sh.200. Find the cost of making the following announcement.

THE GENERAL ELECTRAL COMMISSION INFORMS THE PUBLIC THAT THE PRESIDENTIAL AND PARLIAMENTARY ELECTIONS WILL TAKE PLACE ON EIGHTEENTH FEBRUARY 2011,
THE VOTER ARE THEREFORE REMINDED TO CHECK FOR THEIR NAMES IN THE REGISTERS TO AVOID ANY INCONVINIENCES DURING THE ELECTION DAY.
$\qquad\qquad\qquad\qquad\qquad\qquad\qquad$ CHAIRMAN ELECTORAL COMMISSION.

Total number of words	= 44
Cost of 1st 25 words	= 1500/=
Remaining words	= 44 – 25
	= 19

Cost of 19 words	= 19 x 200/=
	= 3800/=

Total cost of 44 words	= 1500/= + 3800/=
	= 5300/=

POSTAGE RATES .

1. Below are postage charges.

1ST UNIT OR LESS (30G) 600/=

Each addition unit   300/=

Printed papers

1st unit or less (50g)   300/=

Each addition unit   200/=

a) Find cost of posting a letter weighing 175g

Solution

Total number of units   = 175g

30g

= 5 5/6

= 6units

Cost of 1st unit   = 600/=

Remaining units   = 6 – 1

= 5

Cost of 5 units   = 5 x 300/=

= 1500/=

Total cost of 6 words   = 600/= + 1500/=

= 2100/=

b) Find the cost of posting a letter weighing 150g and 2printed papers each weighing 300g

Cost of a letter weighing 150g

Total number of units in 150g   = 150g

30g

= 5 units

Cost of 1st unit   = 600/=

Cost of 4 units   = 4 x 300
                        = 1200/=
Cost of 5 units   = 600 + 1200
                        = 1500/=

Cost of printed papers weighing   = 300g
Total number of units in 300g   = $\frac{300g}{50g}$

                                          = 6 units

Cost of 1st unit   = 300/=
Cost of 5 units   = 5 x 200/=
                      = 1000/=

Total cost of 6 units = 1000/= + 300/=
                        = 1300/=

Total cost of 2 printed papers each weighing 300g   = 1300 x 2
                                                   = 2600/=
Total cost   = 1800/=
                +2600/=
               4400/=